# Latent Space Factorisation and Manipulation via Matrix Subspace Projection

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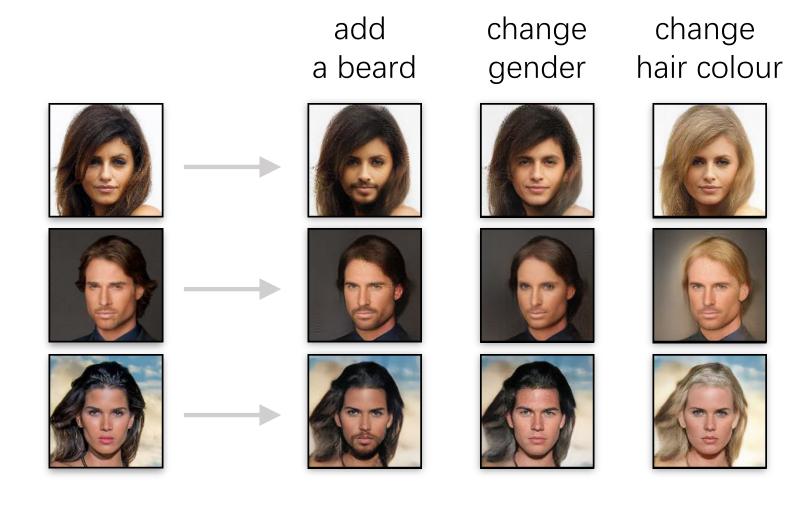








# Manipulating the Attributes of Data (image example)









# Manipulating the Attributes of Data (text example)

set
EatType = coffee shop

set Near = Avalon

the blue spice pub, near crowne plaza hotel, has a customer rating of 5 out of 5.



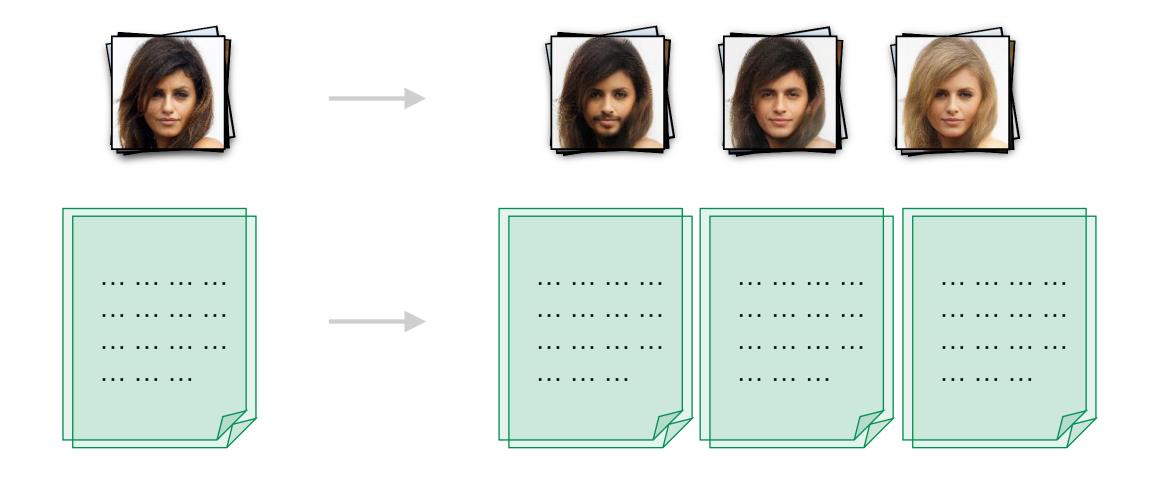
the blue spice pub, near avalon, has a customer rating of 5 out of 5.







# Manipulating the Attributes of Data (text example)



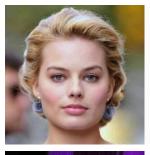


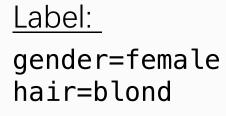


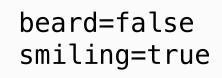


## Training Dataset (CelebA)

# Examples







glasses=true



<u>Label:</u>
gender=male
hair=black

beard=true
smiling=true

glasses=true

•••



<u>Label:</u>
gender=female
hair=brown

<sup>\*</sup>Each pic has 40 labels







# Training Dataset (CelebA.)

Label: gender=female and earring=true



Lot of

Label: gender=male and earring=true



Rare

Label: gender=female and beard=true



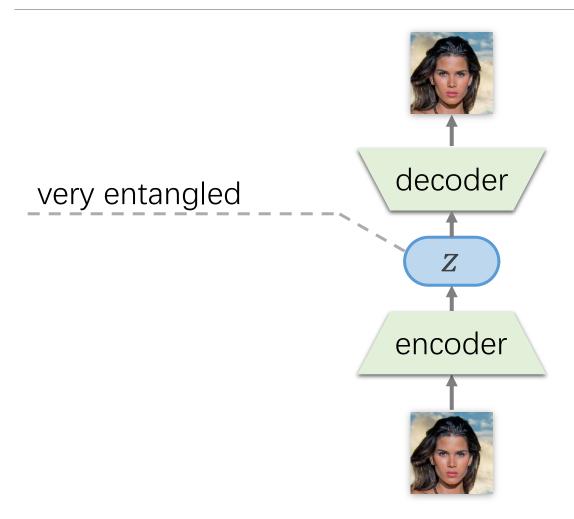
Never seen!







# A Typical Autoencoder (without MSP)

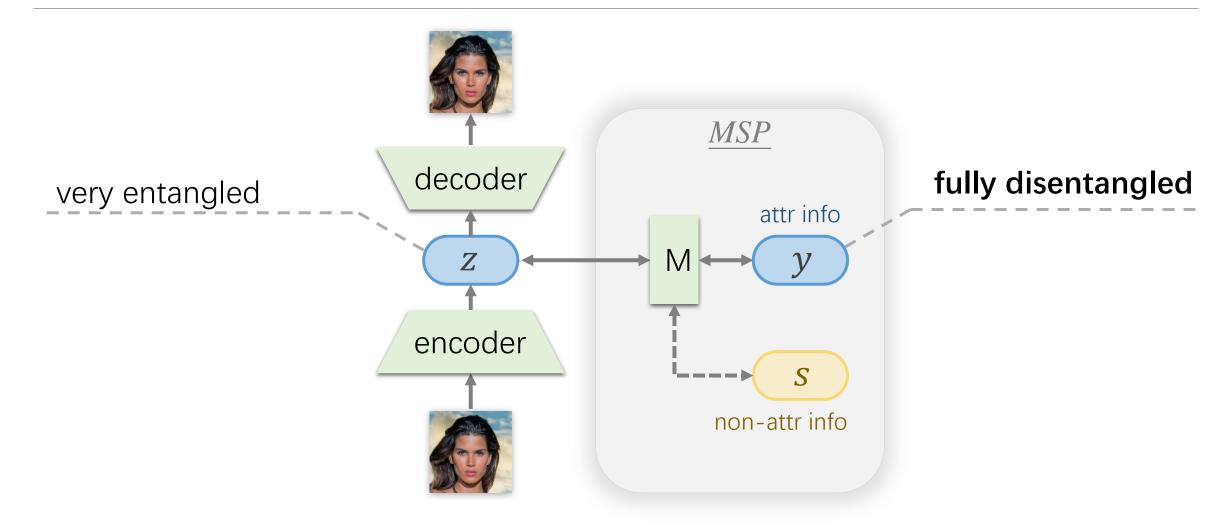








#### Autoencoder with MSP

















Lample, G., Zeghidour, N., Usunier, N., Bordes, A., De-noyer, L., et al. Fader networks: Manipulating images by sliding attributes. InAdvances in Neural InformationProcessing Systems, pp. 5967–5976, 2017.























5 0'clock shadow is removed and make-up is added!

Lample, G., Zeghidour, N., Usunier, N., Bordes, A., De-noyer, L., et al. Fader networks: Manipulating images by sliding attributes. InAdvances in Neural InformationProcessing Systems, pp. 5967–5976, 2017.

Although Fader Networks is capable for multiple attribute editing with one model, in practice, multiple attribute setting makes the results blurry.

-- He et al. (2019)







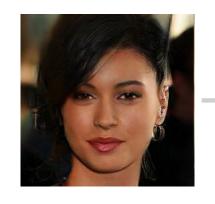
Lample, G., Zeghidour, N., Usunier, N., Bordes, A., De-noyer, L., et al. Fader networks: Manipulating imagesby sliding attributes. InAdvances in Neural InformationProcessing Systems, 2017.





5 0'clock shadow is removed and make-up is added!

Wu, P.-W., Lin, Y.-J., Chang, C.-H., Chang, E. Y., and Liao, S.-W. Relgan: Multidomain image-to-image translation via relative attributes. In The IEEE International Conference on Computer Vision (ICCV), October 2019.





significant changes in skin colour, eyebrows, eyes, and lips











the face has four eyebrows!

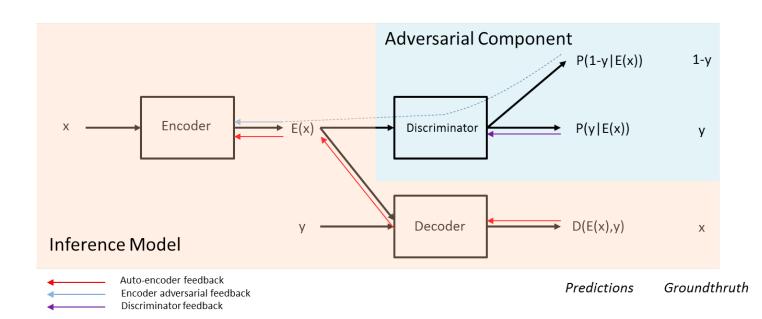
A further problem with many other works that use skip connections.

The face was changed from female to male. New bushy male eyebrows were added, but the skip connections also preserved the original feminine eyebrows in their original position.









Lample, G., Zeghidour, N., Usunier, N., Bordes, A., De-noyer, L., et al.

#### Fader networks:

Manipulating images by sliding attributes. InAdvances in Neural InformationProcessing Systems, 2017.



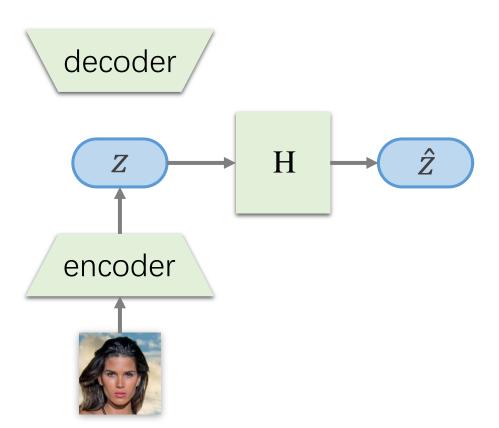


# Methodology





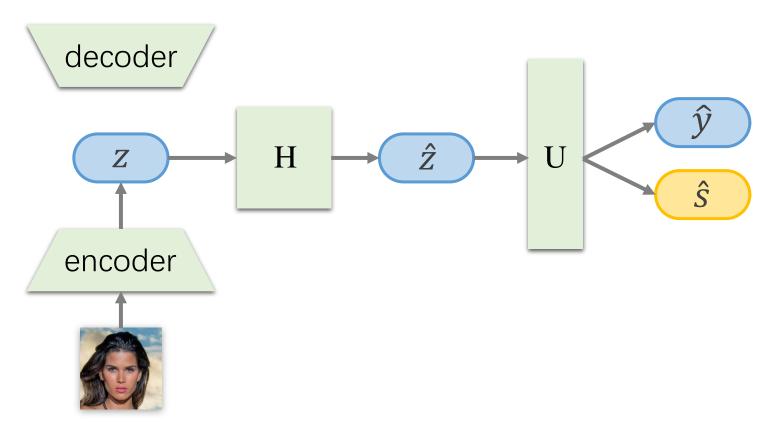








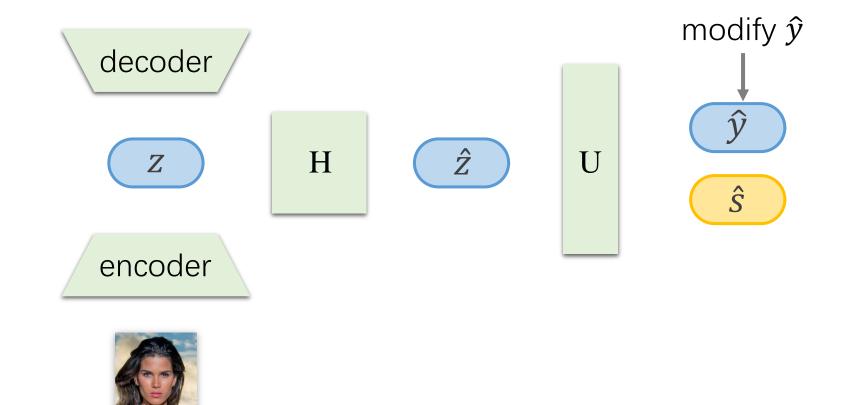








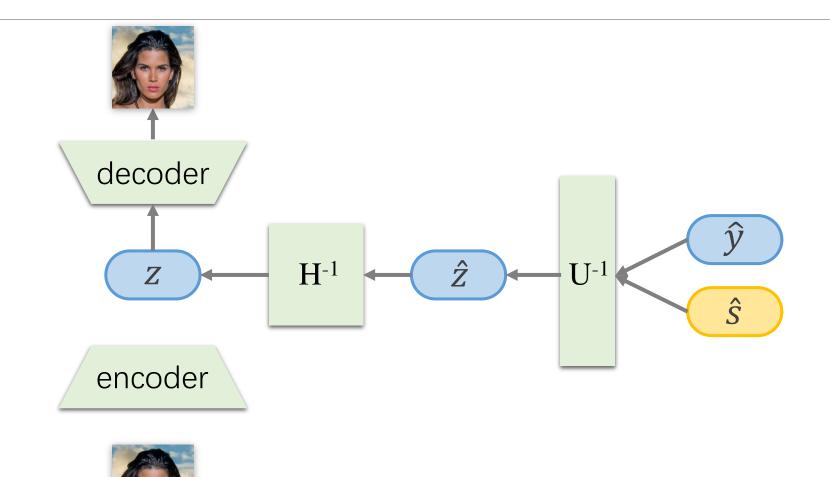










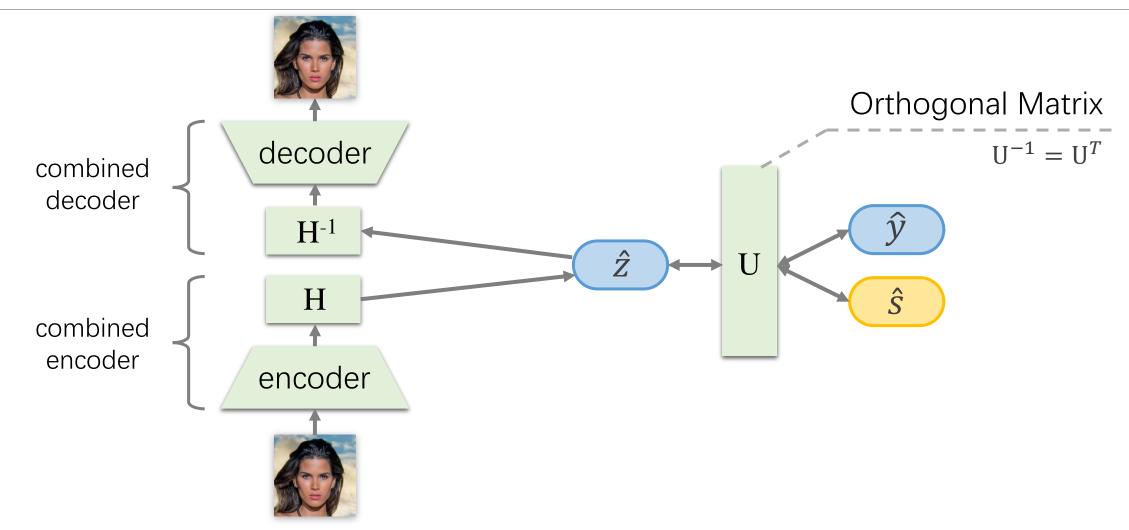








#### Combined Encoder and Decoder

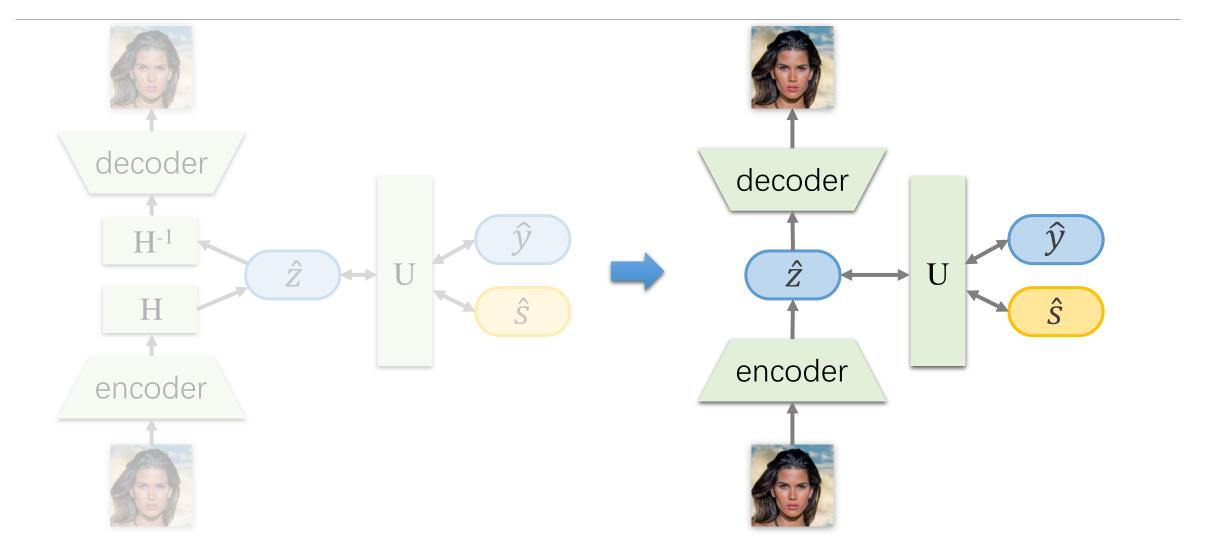








#### Combined Encoder and Decoder



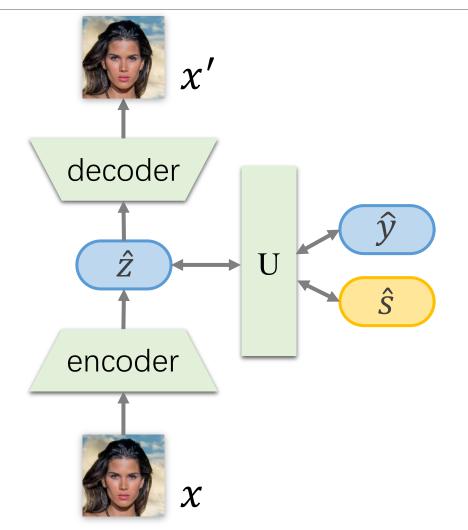






• The produced image should be close to the input as much as possible:

$$\mathcal{L}_{AE} = \|x' - x\|^2$$



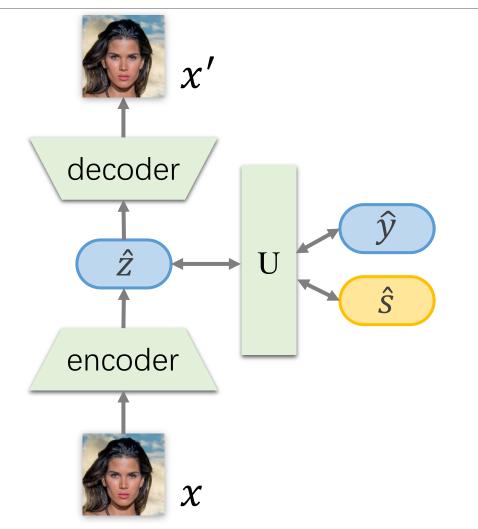






• The predicted attributes should be close to the given attributes:

$$\mathcal{L}_1 = \|\hat{y} - y\|^2$$



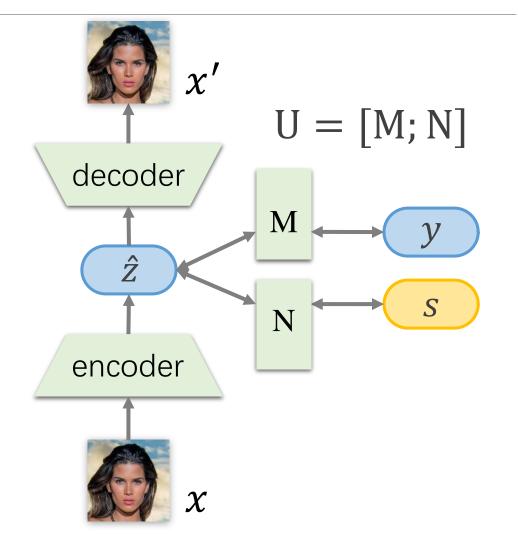






• The predicted attributes should be close to the given attributes:

$$\mathcal{L}_1 = \|\hat{y} - y\|^2$$
$$= \|\mathbf{M} \cdot \hat{z} - y\|^2$$









• \$\hat{s}\$ contains as little information from \$\hat{z}\$ as possible:

$$\mathcal{L}_{2} = \|\hat{s}\|^{2}$$

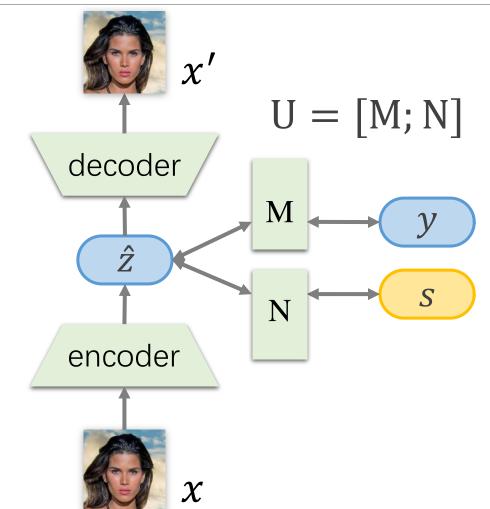
$$= \|\hat{s} - 0\|^{2}$$

$$= \|[\hat{y}; \hat{s}] - [\hat{y}; 0]\|^{2}$$

$$= \|U \cdot \hat{z} - [\hat{y}; 0]\|^{2}$$

• When U is orthogonal (more later):

$$\mathcal{L}_2 = \left\| z - \mathbf{M}^{\mathrm{T}} \cdot \hat{\mathbf{y}} \right\|^2 \approx \left\| z - \mathbf{M}^{\mathrm{T}} \cdot \mathbf{y} \right\|^2$$









• The total loss is:

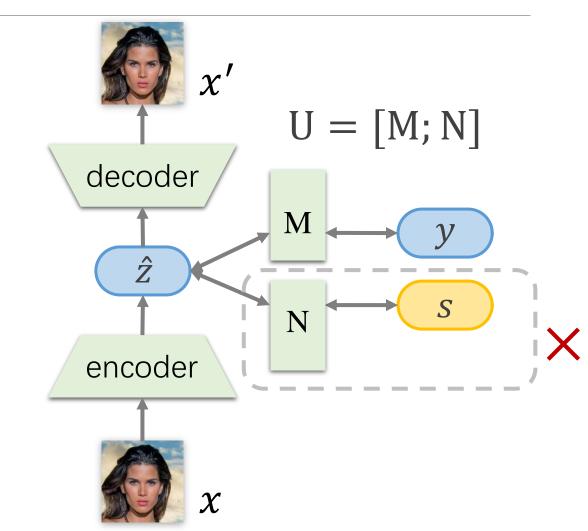
$$\mathcal{L} = \mathcal{L}_{AE} + \mathcal{L}_{1} + \mathcal{L}_{2}$$

$$= \|x' - x\|^{2}$$

$$+ \|M \cdot \hat{z} - y\|^{2}$$

$$+ \|z - M^{T} \cdot \hat{y}\|^{2}$$

\$\hat{s}\$ does not appear in the total loss, so we don't need to learn N!

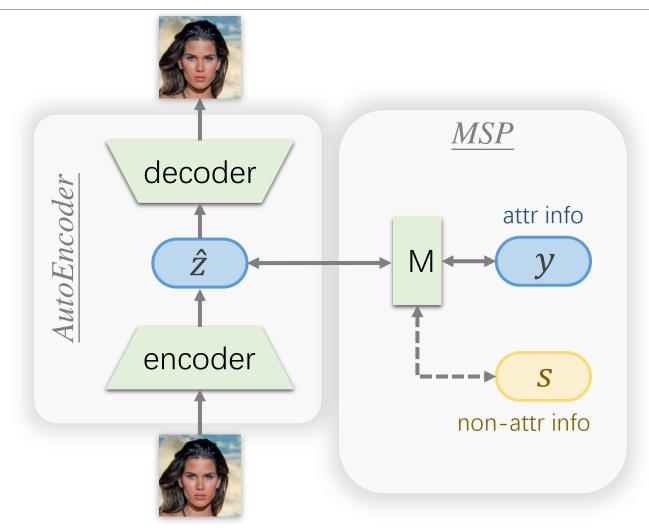








#### Autoencoder with MSP









# Evaluation







# Picture Interpolation Generated by MSP

• Gender - Beard interpolations

female without beard

female with beard

male with beard

male without beard

female without beard









# Picture Interpolation Generated by MSP

• Mouth open - Smiles interpolations

mouth closed and no smile

mouth open and no smile

mouth open and smile

mouth closed and smile

mouth closed and no smile







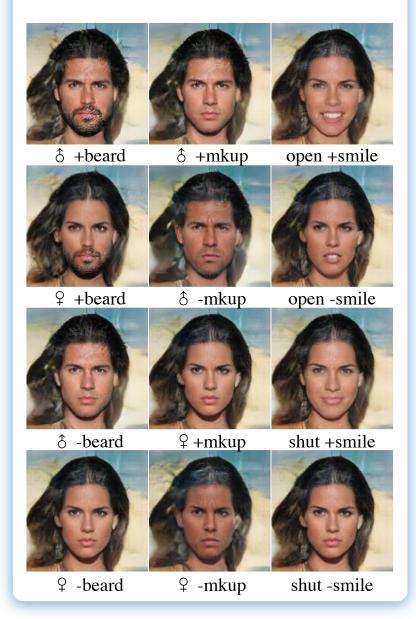


# Picture Interpolation Generated by MSP

- Multiple attribute interpolations including:
  - glasses
  - beard
  - hair colour
  - narrow eyes
  - mouth open



#### **MSP**



baseline Fader Networks

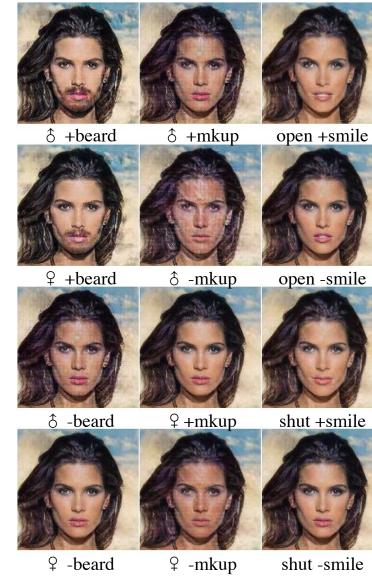


















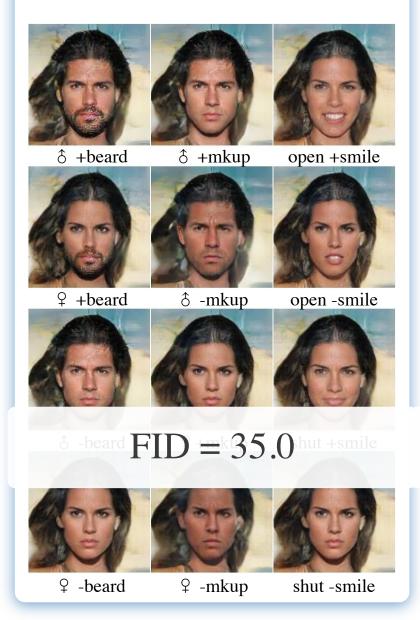
### Quantitative Evaluation

	MSP(ours)	Fader	AttGAN
male x beard	0.78	0.42	0.45
female x beard	0.52	0.03	0.41
male x no-beard	0.86	0.40	0.42
female x no-beard	0.90	0.61	0.63
male x makeup	0.52	0.02	0.35
male x no-makeup	0.89	0.50	0.47
female x makeup	0.87	0.63	0.52
female x no-makeup	0.67	0.42	0.47
smile x open-mouth	0.89	0.59	0.63
no-smile x open-mouth	0.66	0.11	0.29
smile x calm-mouth	0.95	0.34	0.33
no-smile x calm-mouth	0.76	0.43	0.38
male x bald	0.78	0.10	0.29
male x bangs	0.56	0.05	0.19
female x bald	0.29	0.01	0.17
female x bangs	0.68	0.21	0.20
no-glasses x black-hair	0.74	0.38	0.53
no-glasses x golden-hair	0.86	0.36	0.79
glasses x black-hair	0.82	0.21	0.32
glasses x golden-hair	0.77	0.19	0.33

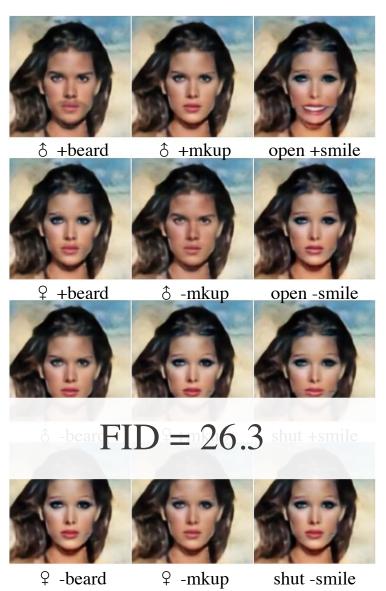
■ MSP (ours) AttGan Fader 0.9 8.0 0.7 0.6 0.5 0.4 0.3 0.2 0.1 no snile topen mouth no-smile \* calm-mouth noglasses teolden hair kemale + no. beard male thomakeup remale + makeup smile topen mouth no disses to back hair temale + banes alasses t bladt hair male + nor beard snile + calminouth tende toold diases teolden nair rnale + bald male + banes

*Table 2.* The classification accuracy of generated images using MSP, Fader Networks and AttGAN.

#### **MSP**



#### baseline Fader Networks

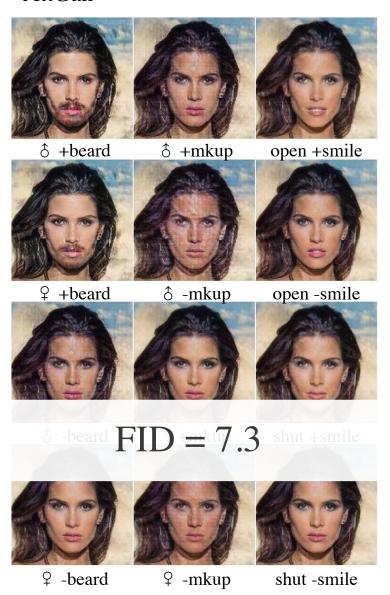


baseline AttGan















#### Human Evaluation

	MSP(ours)	Fader	AttGAN
male x beard	0.78	0.42	0.45
female x beard	0.52	0.03	0.41
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*Table 2.* The classification accuracy of generated images using MSP, Fader Networks and AttGAN.

male / beard attributes morphing			
	Fader	AttGAN	VAE+GAN
	Network		MSP
perfect	38.3%	55.9%	74.4%
recognizable	8.3%	11.2%	11.6%
unreco/unchang	53.3%	32.9%	14.0%

mouth open / smiling attributes morphing			
	Fader	AttGAN	VAE+GAN
	Network		MSP
perfect	36.7%	47.5%	68.3%
recognizable	20.8%	15.3%	4.9%
unreco/unchang	42.5%	37.2%	26.8%

Table 4. Manual valuation results of disentanglement. Numbers in the table denote percentage of participants under the column heading who felt the images represented the specified attribute (e.g. smiling) in a way that was perfect, recognisable, or unrecognisable/unchanged.







## Evaluation (textural task)

- E2E dataset.
- A classic seq2seq autoencoder (lstm-lstm) + MSP

	Example 1	Example 2
Orig-attribute	eatType[pub], customer-rating[5-out-of-5],	familyFriendly[yes], area[city-centre], eatType[pub],
	name[Blue-Spice], near[Crowne-Plaza-Hotel]	food[Japanese], near[Express-by-Holiday-Inn],
		name[Green-Man]
Orig-text	the blue spice pub, near crowne plaza hotel,	near the express by holiday inn in the city centre is green
	has a customer rating of 5 out of 5.	man . it is a japanese pub that is family-friendly .
New-attribute	eatType[coffee-shop], customer-rating[5-out-	familyFriendly[no], area[riverside], eatType[coffee-shop],
	of-5], name[Blue-Spice], near[Avalon]	food[French], near[The-Six-Bells], name[Green-Man]
New-text	the blue spice coffee shop, near avalon has a	near the six bells in the riverside area is a green man . it is
	customer rating of 5 out of 5.	a french coffee shop that is not family-friendly.



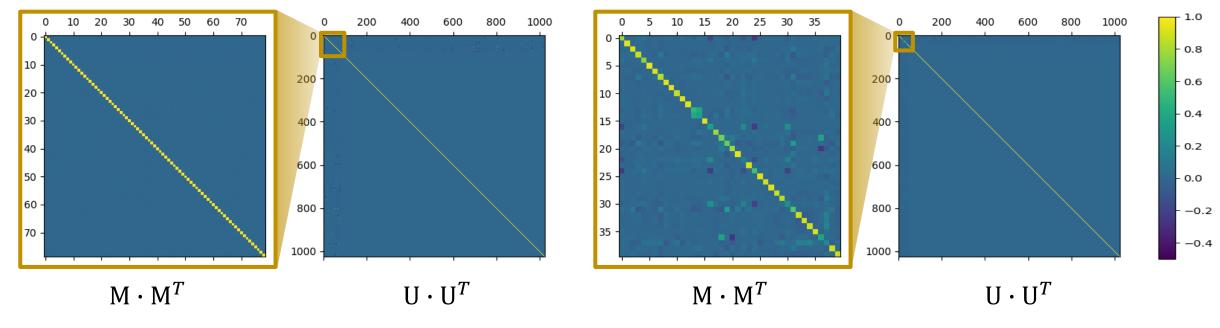




# Orthogonality of U

• Since  $\mathcal{L}_2$  uses the orthogonality of U, do we train U as an orthogonal matrix? Almost!

(MSP only learns M, but can obtain U by calculating the *null space* of M)



for the E2E dataset

for the CelebA dataset







# Conclusion







#### Conclusion

- We proposed MSP, which fully disentangles the latent space of an autoencoder to manipulate the multiple attributes in the latent space.
- Our model is a plug-in, which in principle can be attached to any type of autoencoder (e.g. for images or text), and we have a principled weighting strategy for combining the loss terms for training.
- MSP shows strong performance on learning disentangled latent representations of multiple attributes.
- We also suggested a way to train a matrix to be orthogonal.







# Thanks!

The code of MSP and relative data is here: https://xiao.ac/proj/msp