



# Bayesian Optimization Meets Bayesian Optimal Stopping

Zhongxiang Dai <sup>1</sup>

Haibin Yu <sup>1</sup>

Bryan Kian Hsiang Low <sup>1</sup>

Patrick Jaillet <sup>2</sup>

<sup>1</sup> Department of Computer Science, National University of Singapore

<sup>2</sup> Department of Electrical Engineering and Computer Science, Massachusetts Institute of Technology

**Machine Learning** (ML) models have achieved unprecedented level of performances

**Problem:**

Choice of **hyperparameters**

- **Reason:** high computational cost



**Solution:**

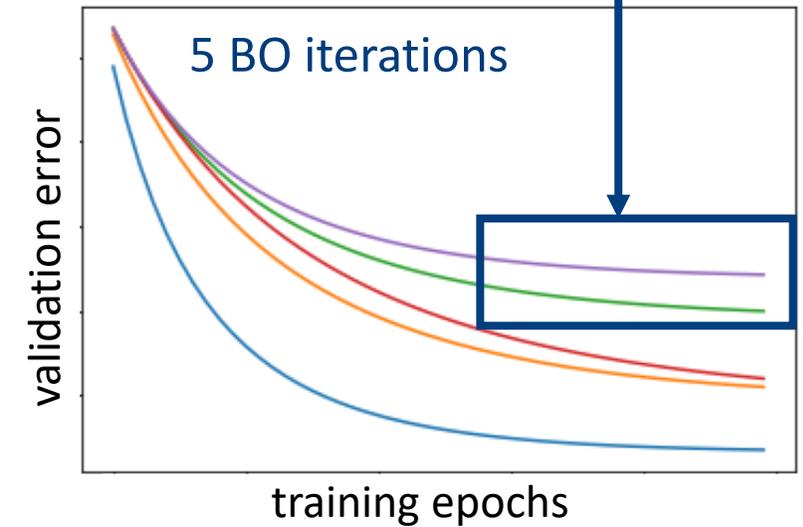
**Bayesian Optimization (BO)**

- **Sample efficiency:** requires a small number of function evaluations
- **Theoretical guarantee:** Gaussian Process-Upper Confidence Bound (**GP-UCB**)

- Many ML models require *iterative training*
  - e.g. stochastic gradient descent (neural network)



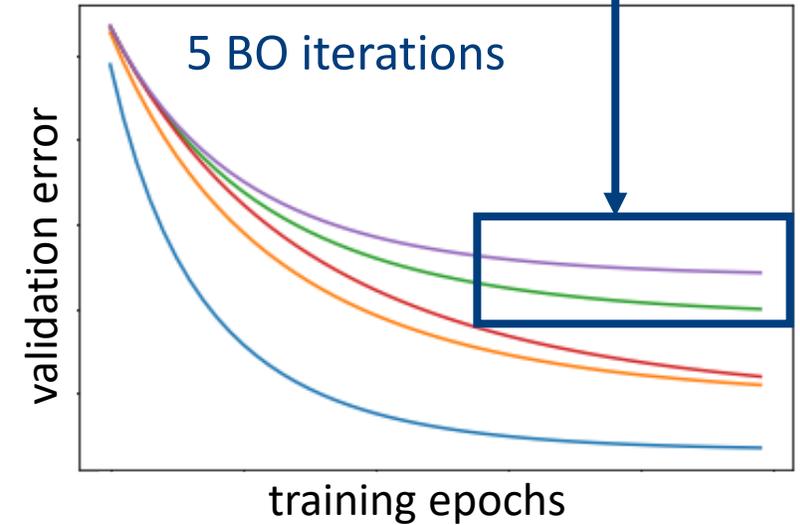
**wasted  
computation**



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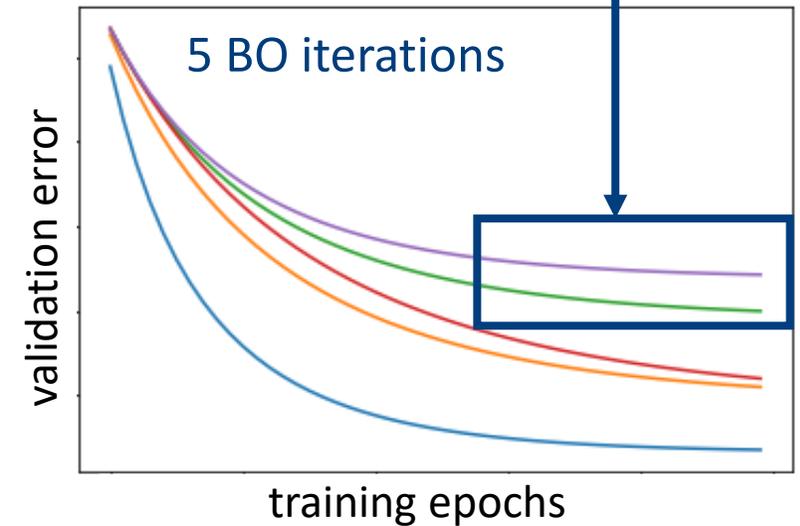
**Can we early-stop unpromising  
hyperparameters to save resource?**

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**wasted  
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**Can we early-stop unpromising  
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**a principled optimal stopping  
rule is needed**

**Bayesian Optimal Stopping (BOS)**

- **Contribution**

- We propose **BO-BOS**, which unifies BO (GP-UCB) and BOS to achieve epoch-efficient hyper-parameter tuning
- We show that BO-BOS is **asymptotically no-regret** and performs effectively in practice

# The BO-BOS Algorithm

- for  $t = 1, 2 \dots$ 
  - choose the hyperparameter  $\mathbf{x}_t$  to query by maximizing the GP-UCB acquisition function

# The BO-BOS Algorithm

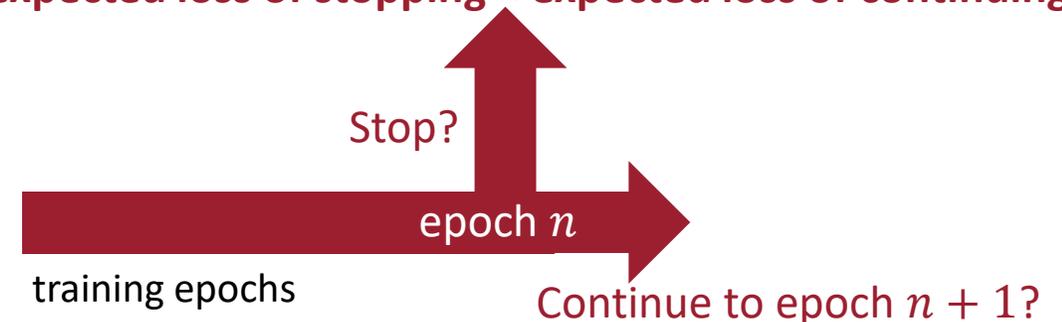
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  - Formulate & solve the **BOS** problem

# The BO-BOS Algorithm

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  - Formulate & solve the **BOS** problem
  - Train the ML model using  $\mathbf{x}_t$ , early-stop the training **if BOS outputs the stopping decision**

**BOS outputs the stopping decision if  $\mathbf{x}_t$  is believed to end up performing worse than the currently found optimum**

expected loss of stopping < expected loss of continuing

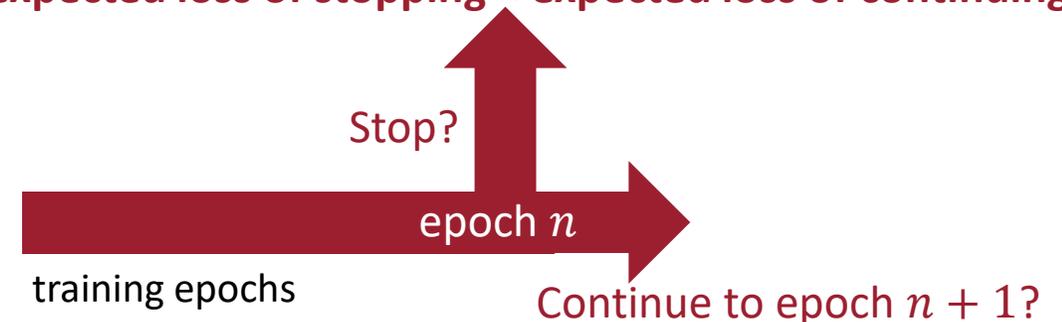


# The BO-BOS Algorithm

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  - Formulate & solve the **BOS** problem
  - Train the ML model using  $\mathbf{x}_t$ , early-stop the training **if BOS outputs the stopping decision**
  - Update Gaussian process belief of the objective function

**BOS outputs the stopping decision if  $\mathbf{x}_t$  is believed to end up performing worse than the currently found optimum**

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# Theoretical Analysis

- BO aims to minimize the **simple regret**:  $S_T \triangleq f(\mathbf{z}^*) - \max_{t \in \{1, \dots, T\}} f(\mathbf{z}_t)$

expectation over the uncertainty introduced by BOS

$$\mathbb{E}[S_T] \leq \frac{\kappa \sqrt{TC_1 \beta_T \gamma_T}}{T} + \frac{\sum_{t=1}^T \eta_t}{T} + \frac{1}{T} Nb \sqrt{\log \frac{da}{\delta'} \tau_T}$$

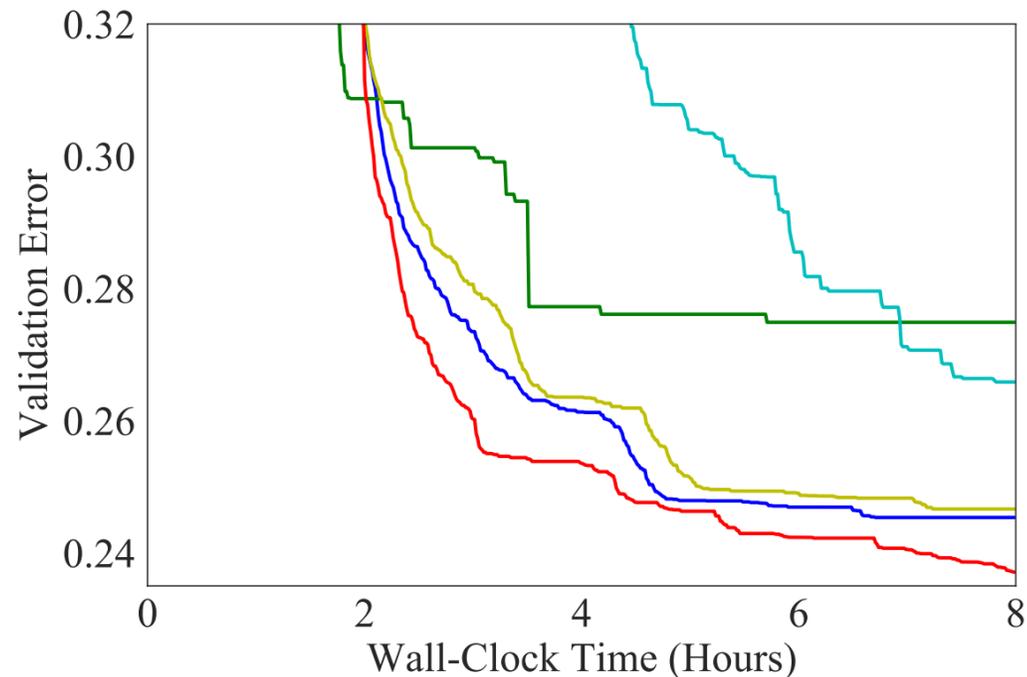
- Matches the simple regret of GP-UCB, thus asymptotically vanishes

- **Asymptotically vanish** if the BOS parameters are chosen with consideration of the **exploration vs. exploitation trade-off**

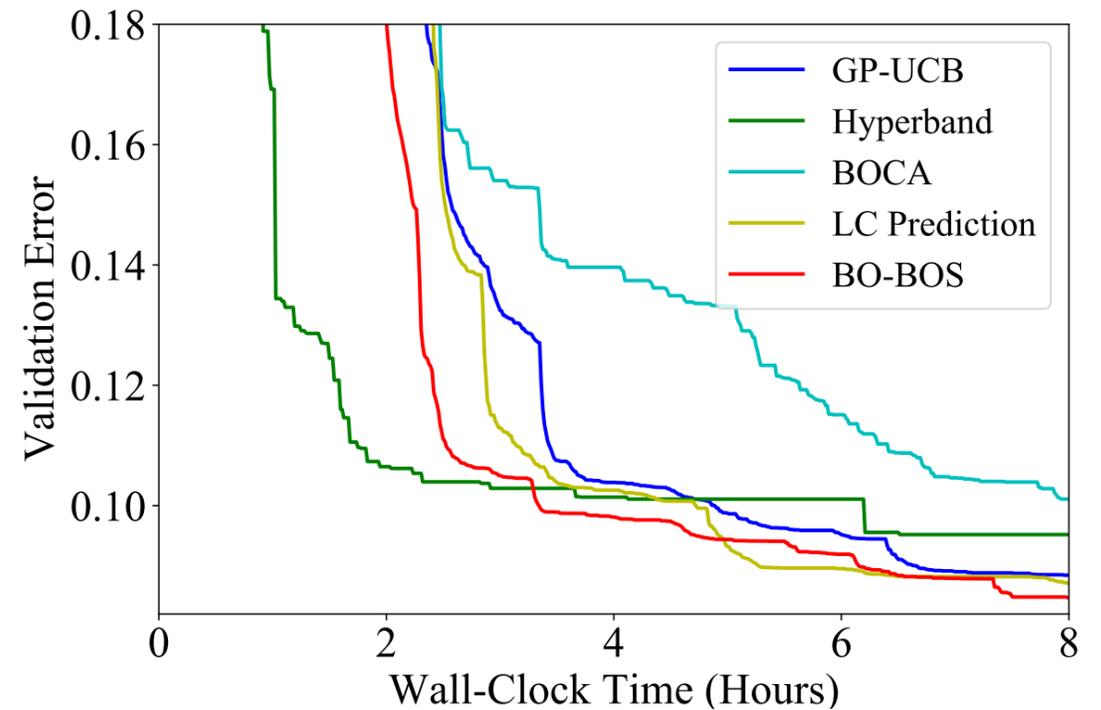
# Experiments

- Hyperparameter Tuning
  - Convolutional Neural Networks

CIFAR-10 dataset

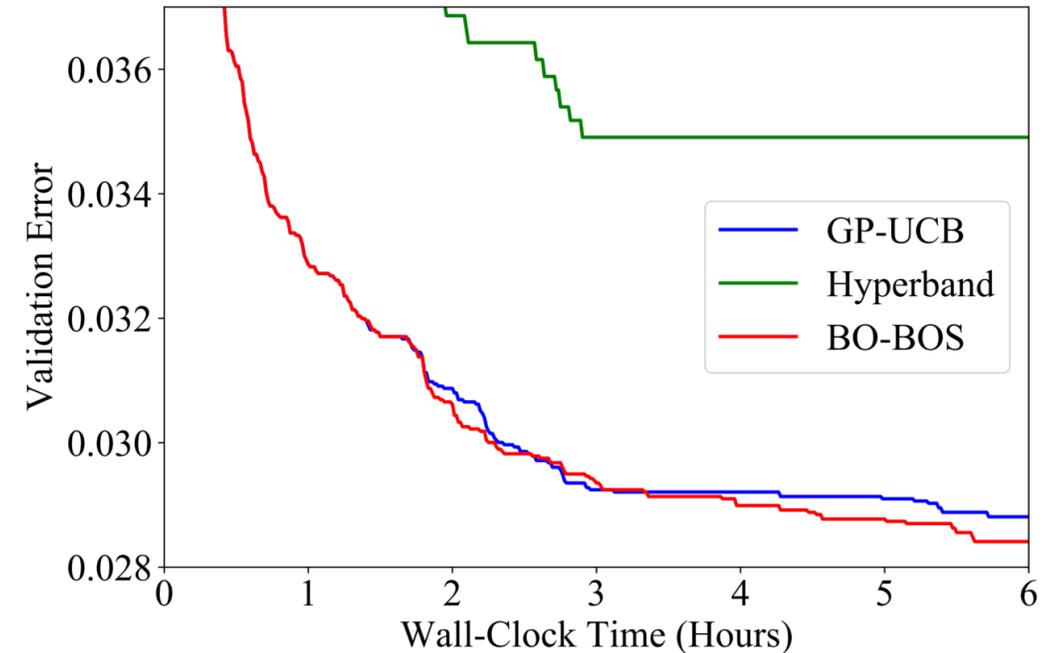
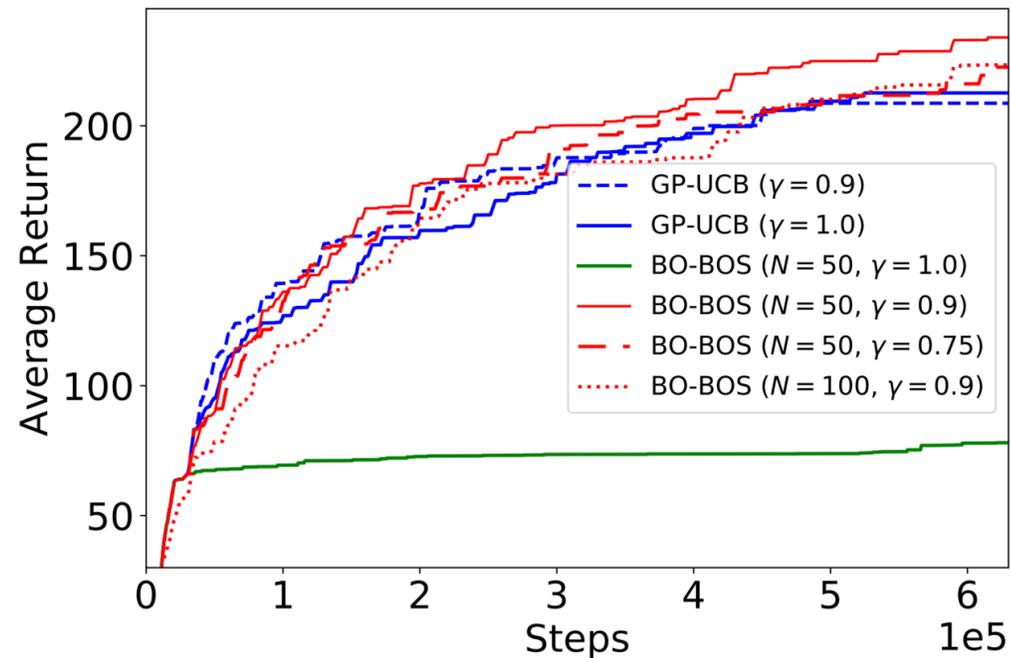


SVHN dataset



# Experiments

- Beyond Hyperparameter Tuning:
  - Policy search for Reinforcement Learning (Swimmer-v2 from OpenAI, Mujoco)
  - Joint hyperparameter tuning and feature selection





# Thank you!

For more information, please visit our poster at **Pacific Ballroom #228**