# Flexibly Fair Representation Learning by Disentanglement

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## Why Fair Representation Learning?

Fair Representation: 
$$[\mathbf{x}, \mathbf{a}] \stackrel{f}{\to} \mathbf{z} \stackrel{g_1}{\to} \hat{y}_1$$

$$\mathbf{z} \stackrel{g_2}{\to} \hat{y}_2$$

$$\mathbf{z} \stackrel{g_3}{\to} \hat{y}_3$$

Given sensitive attribute  $a \in \{0,1\}$ , we want:

- $\mathbf{z} \perp a$  (demographic parity) with  $\mathbf{z} = f(\mathbf{x}, a)$
- z maintains as much info about x as possible

A fair representation acts as a group parity bottleneck

Current approaches are flexible w.r.t. downstream task labels (Madras et al., 2018) but inflexible w.r.t. sensitive attributes

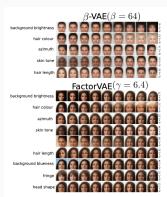
## **Further Motivation**

#### Subgroup discrimination

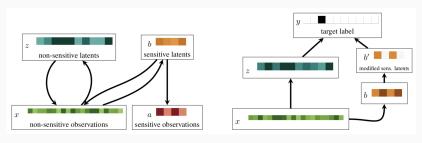
- We would like to handle the case where  $\mathbf{a} \in \{0,1\}^{N_a}$  is a vector of sensitive attributes
- ML systems can discriminate against subgroups defined via conjunctions of sensitive attributes (Buolamwini & Gebru, 2018)

### **Disentangled Representation Learning**

- Each dimension of z should correspond to no more than one semantic factor of variation (object shape, position, etc.) in the data
- VAE variants encourage factorized posterior q(z|x)
   (Higgins et al., 2017) or aggregate posterior q(z) (Kim & Mnih, 2018; Chen et al., 2018)



## Flexibly Fair VAE



Data flow at train time (left) and test time (right) for FFVAE

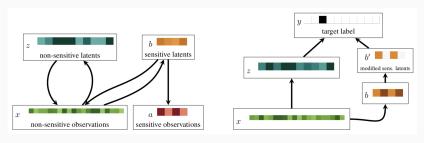
#### Desiderata

- $\mathbf{z} \perp b_i \ \forall j$
- $b_i \perp b_j \ \forall \ i \neq j$
- MutualInfo $(a_j, b_j)$  is large  $\forall j$

#### Latent Code Modification

- To achieve DP w.r.t. some a<sub>i</sub>, use
   [z, b]\b<sub>i</sub>
- To achieve DP w.r.t. conjunction of binary attributes a<sub>i</sub> ∧ a<sub>j</sub> ∧ a<sub>k</sub>, use [z, b]\{b<sub>i</sub>, b<sub>j</sub>, b<sub>k</sub>}

## Flexibly Fair VAE



Data flow at train time (left) and test time (right) for FFVAE

### **Learning Objective**

$$\begin{split} L_{\text{FFVAE}}(p,q) &= \mathbb{E}_{q(\mathbf{z},\mathbf{b}|\mathbf{x})}[\log p(\mathbf{x}|\mathbf{z},\mathbf{b}) + \alpha \sum_{j} \log p(a_{j}|b_{j})] \\ &- \gamma D_{KL}(q(\mathbf{z},\mathbf{b})||q(\mathbf{z}) \prod_{j} q(b_{j})) \\ &- D_{KL}[q(\mathbf{z},\mathbf{b}|\mathbf{x})||p(\mathbf{z},\mathbf{b})] \end{split}$$

 $\alpha$  encourages predictiveness in the latent code;  $\gamma$  encourages disentanglement

## Results - Synthetic Data

## **DSpritesUnfair**



Figure: With correlated factors of variation, a fair classification task is predicting Shape without discriminating against XPosition

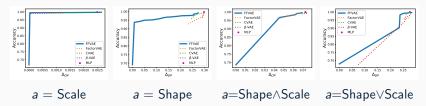
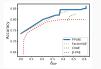


Figure: Pareto-fronts showing fairness-accuracy tradeoff curves, DSpritesUnfair dataset. Optimal point is top left corner (perfect accuracy, no unfairness). y = XPosition.

$$\Delta_{DP} \triangleq |\mathbb{E}[\hat{y} = 1|a = 1] - \mathbb{E}[\hat{y} = 1|a = 0]| \text{ with } \hat{y} \in \{0, 1\}$$

## Results - Tabular and Image Data

#### **Communities & Crime**





typical success:  $a = R \land P$ 

typical failure:  $a = R \lor B$ 

- Neighborhood-level population statistics: 120 features for 1,994 neighborhoods
- We choose racePctBlack (R), blackPerCap (B), and pctNotSpeakEnglWell (P) as sensitive attributes
- Held-out label
   y = violentCrimesPerCapita

#### Celeb-A





typical success:  $a = \neg E \land M$ 

typical failure:  $a = C \wedge M$ 

- Over 200, 000 images of celebrity faces, each associated with 40 binary attributes (OvalFace, HeavyMakeup, etc.)
- We choose Chubby (C), Eyeglasses
   (E) and Male (M) as sensitive attributes
- Held-out labely = HeavyMakeup (H)

## Conclusion

- FFVAE enables flexibly fair downstream classification by disentangling information from multiple sensitive attributes
- Future work: extending to other group fairness definitions, and studying robustness of disentangled/fair representation learners to distribution shift
- Visit us at poster # 131 tonight!