

Mining Large Graphs: Patterns, Anomalies, and Fraud Detection

Christos Faloutsos
CMU



Thank you!



• Nina Balcan



• Kilian Weinberger



Roadmap



- Introduction Motivation
 - Why study (big) graphs?





Conclusions







~1B nodes (web sites)

~6B edges (http links)

'YahooWeb graph'

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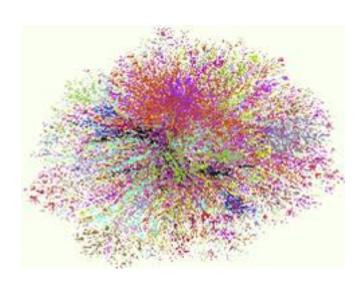


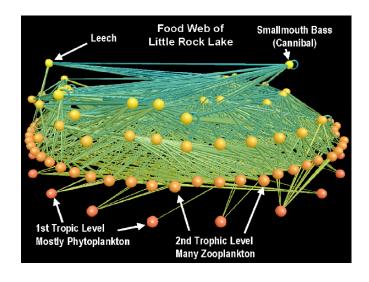
>\$10B; ~1B users



ICML'16







Internet Map [lumeta.com]

Food Web [Martinez '91]

6



- web-log ('blog') news propagation YAHOO! BLOG
- computer network security: email/IP traffic and anomaly detection
- Recommendation systems



•

Many-to-many db relationship -> graph



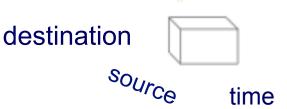
Motivating problems

• P1: patterns? Fraud detection?



• P2: patterns in time-evolving graphs /

tensors





Motivating problems

• P1: patterns? Fraud detection?





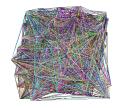


destination source time



Motivating problems

• P1: patterns? Fraud detection?







• P2: patterns in time-evolving graphs / tensors



* Robust Random Cut Forest Based Anomaly Detection on Streams Sudipto Guha, Nina Mishra, Gourav Roy,

Okka Cabrillyara ICMI 146



Roadmap

- Introduction Motivation
 - Why study (big) graphs?





- Part#1: Patterns & fraud detection
- Part#2: time-evolving graphs; tensors
- Conclusions

ICML'16

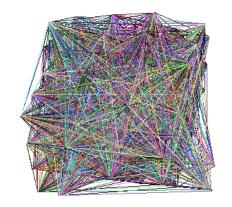


Part 1: Patterns, & fraud detection



Laws and patterns

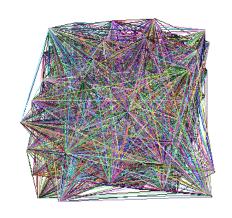
• Q1: Are real graphs random?





Laws and patterns

- Q1: Are real graphs random?
- A1: NO!!
 - Diameter ('6 degrees'; 'Kevin Bacon')
 - in- and out- degree distributions
 - other (surprising) patterns
- So, let's look at the data

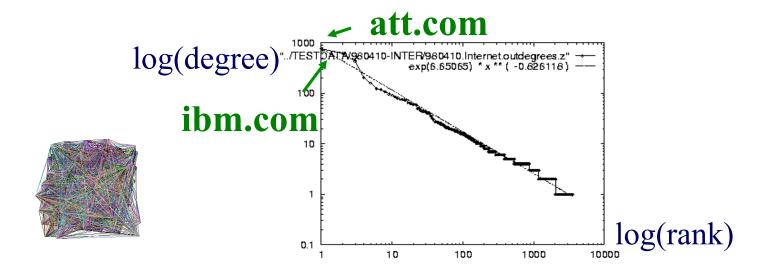






• Power law in the degree distribution [Faloutsos x 3 SIGCOMM99]

internet domains

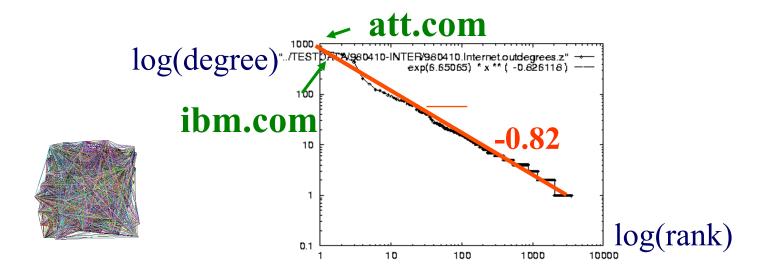


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• Power law in the degree distribution [Faloutsos x 3 SIGCOMM99]

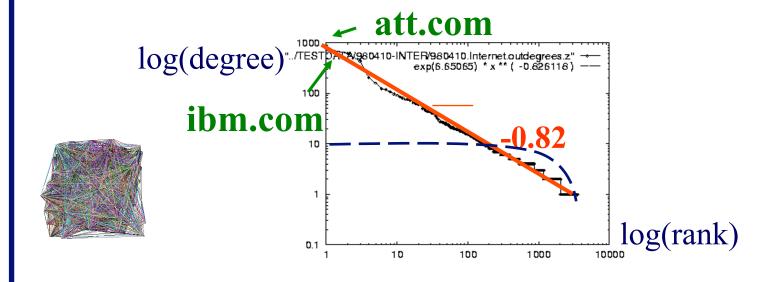
internet domains



ICML'16 (c) 2016, C. Faloutsos 16

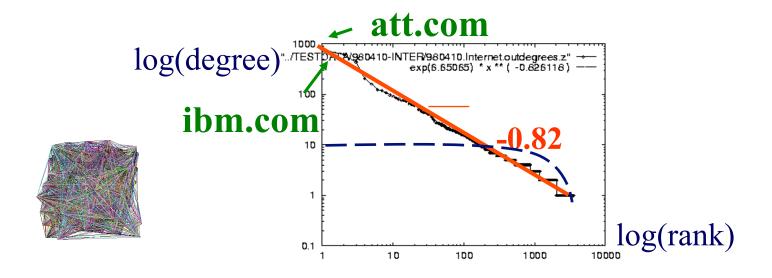
• Q: So what?

internet domains



ICML'16

- Q: So what? = friends of friends (F.O.F.)
- A1: # of two-step-away pairs: internet domains

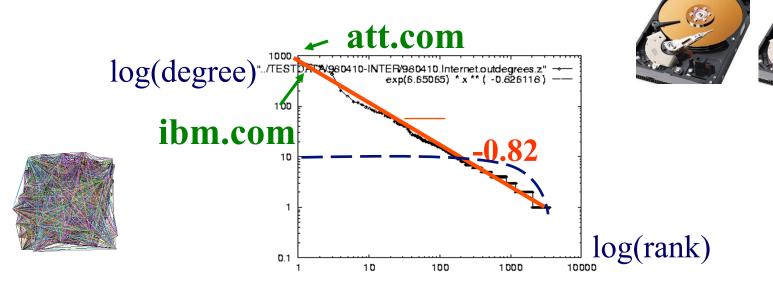


ICML'16

• Q: So what? = friends of friends (F.O.F.)

• A1: # of two-step-away pairs: 100² * N= 10 Trillion

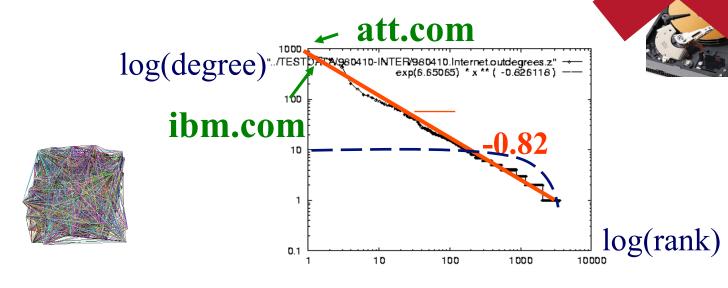




ICML'16



internet domains



ICML'16

Trillion



Gaussian trap

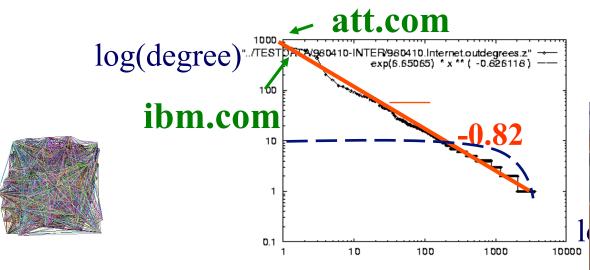
Solution# S.1

= friends of friends (F.O.F.)

• Q: So what?

• A1: # of two-step-away pairs: O(d max 2) $\sim 10M^2$

internet domains



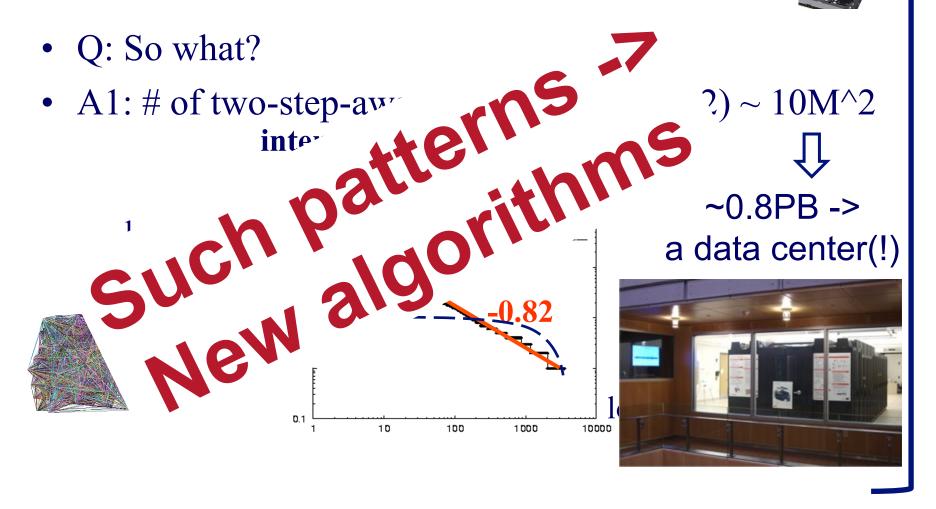
~0.8PB -> a data center(!)





Gaussian trap

Solution# S.1



ICML'16

• $O(N^2)$ algorithms are ~intractable - N=1B

• N^2 seconds = 31B years (>2x age of

universe)

1B

1B

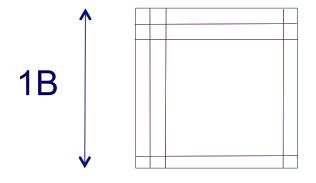


ICML'16

• $O(N^2)$ algorithms are ~intractable - N=1B

31M

- N^2 seconds = 31B years
- 1,000 machines





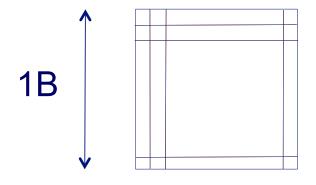


ICML'16

• $O(N^2)$ algorithms are ~intractable - N=1B

31K

- N^2 seconds = 31B years
- 1M machines









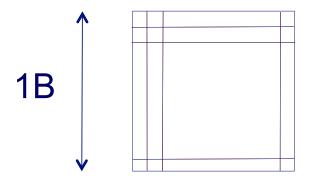
• $O(N^2)$ algorithms are ~intractable - N=1B

3

• N^2 seconds = 31B years



• 10B machines ~ \$10Trillion





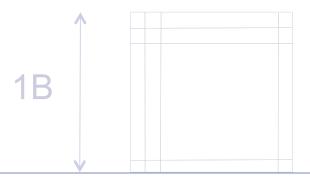
• $O(N^2)$ algorithms are ~intractable - N=1B

And parallelism might not help

• N^2 seconds = 31B years



• 10B machines ~ \$10Trillion



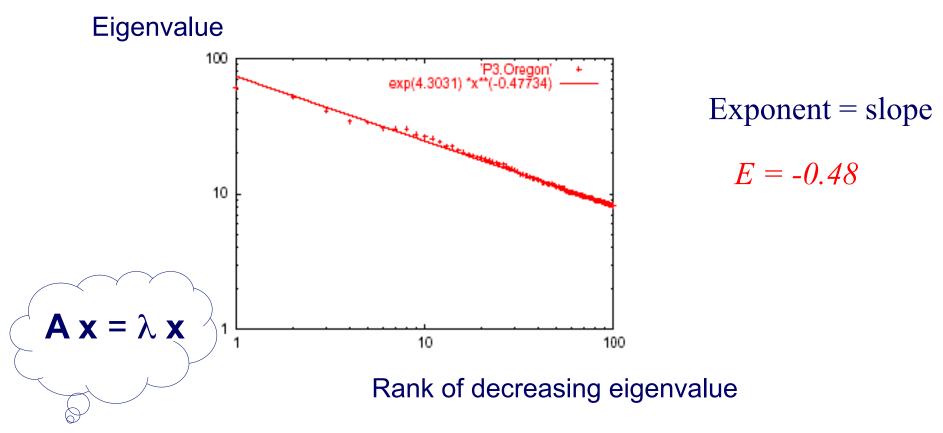






28

Solution# S.2: Eigen Exponent E



• A2: power law in the eigenvalues of the adjacency matrix ('eig()')

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Roadmap

- Introduction Motivation
- Part#1: Patterns in graphs



- Patterns: Degree; Triangles
- Anomaly/fraud detection
- Graph understanding
- Part#2: time-evolving graphs; tensors
- Conclusions





Solution# S.3: Triangle 'Laws'

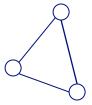


• Real social networks have a lot of triangles

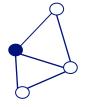
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Solution# S.3: Triangle 'Laws'

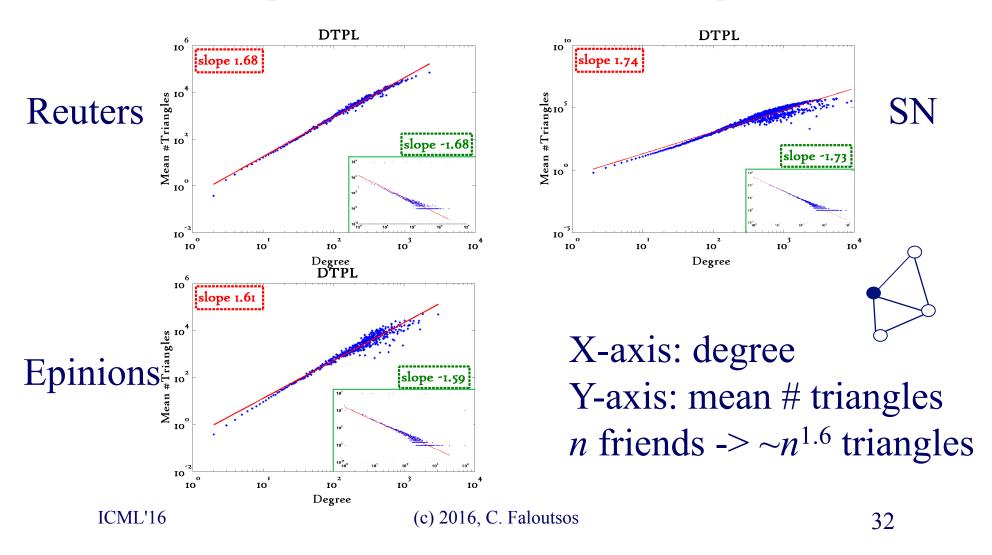


- Real social networks have a lot of triangles
 - Friends of friends are friends
- Any patterns?
 - 2x the friends, 2x the triangles?



ICML'16

Triangle Law: #S.3 [Tsourakakis ICDM 2008]







Triangle Law: Computations

[Tsourakakis ICDM 2008]



But: triangles are expensive to compute

(3-way join; several approx. algos) – $O(d_{max}^2)$

Q: Can we do that quickly?

A:

ICML'16



details

 $\mathbf{A} \mathbf{x} = \lambda \mathbf{x}$

Triangle Law: Computations

[Tsourakakis ICDM 2008]



But: triangles are expensive to compute

(3-way join; several approx. algos) – $O(d_{max}^2)$

Q: Can we do that quickly?

A: Yes!

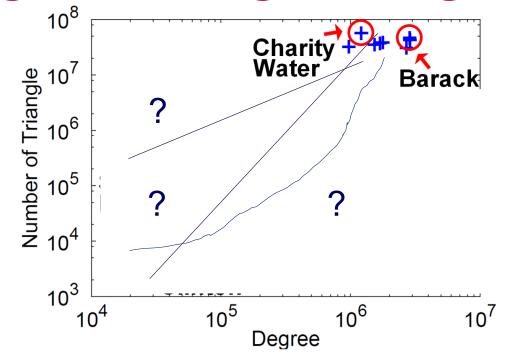
#triangles = 1/6 Sum (λ_i^3)

(and, because of skewness (S2),

we only need the top few eigenvalues! - O(E)



Triangle counting for large graphs?







Anomalous nodes in Twitter(~ 3 billion edges)

[U Kang, Brendan Meeder, +, PAKDD'11]

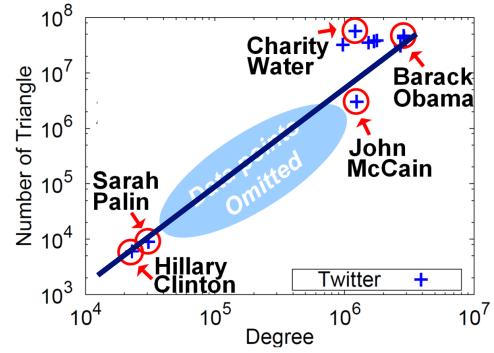
ICML'16







Triangle counting for large graphs?





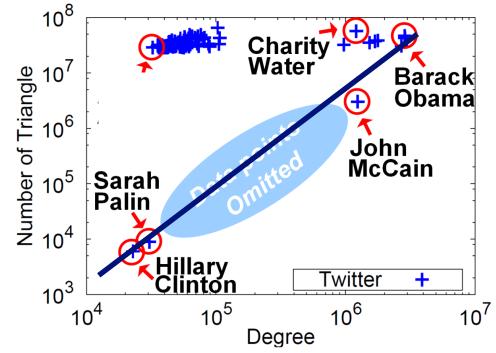


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ICML'16



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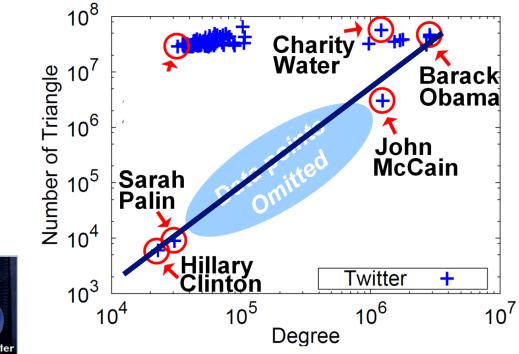
ICML'16



Triangle counting for large graphs?









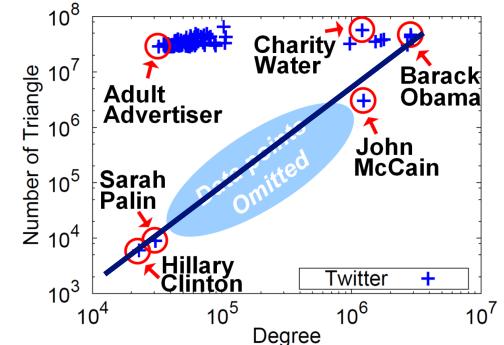


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Triangle counting for large graphs?







39



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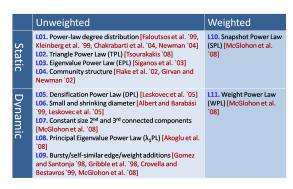
MORE Graph Patterns

| | Unweighted | Weighted |
|---------|--|---|
| Static | Kleinberg et al. '99, Chakrabarti et al. '04, Newman '04] C. Triangle Power Law (TPL) [Tsourakakis '08] C. Eigenvalue Power Law (EPL) [Siganos et al. '03] L04. Community structure [Flake et al. '02, Girvan and Newman '02] | L10. Snapshot Power Law (SPL) [McGlohon et al. `08] |
| Dynamic | L05. Densification Power Law (DPL) [Leskovec et al. `05] L06. Small and shrinking diameter [Albert and Barabási `99, Leskovec et al. `05] L07. Constant size 2nd and 3rd connected components [McGlohon et al. `08] L08. Principal Eigenvalue Power Law (λ₁PL) [Akoglu et al. `08] L09. Bursty/self-similar edge/weight additions [Gomez and Santonja `98, Gribble et al. `98, Crovella and | L11. Weight Power Law (WPL) [McGlohon et al. `08] |

RTG: A Recursive Realistic Graph Generator using Random Typing Leman Akoglu and Christos Faloutsos. PKDD'09.



MORE Graph Patterns



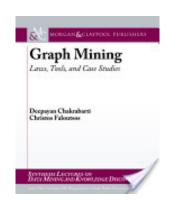
Mary McGlohon, Leman Akoglu, Christos
 Faloutsos. Statistical Properties of Social
 Networks. in "Social Network Data Analytics" (Ed.: Charu Aggarwal)





Deepayan Chakrabarti and Christos Faloutsos,
 <u>Graph Mining: Laws, Tools, and Case Studies</u> Oct.
 2012, Morgan Claypool.





http://www.cs.cmu.edu/~christos/TALKS/16-06-19-ICML/



Roadmap

- Introduction Motivation
- Part#1: Patterns in graphs
 - Patterns
- Anomaly / fraud detection
 - CopyCatch

Patterns >



anomalies

- Spectral methods ('fBox')
- Belief Propagation
- Part#2: time-evolving graphs; tensors
- Conclusions



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Fraud

- Given
 - Who 'likes' what page, and when
- Find
 - Suspicious users and suspicious products

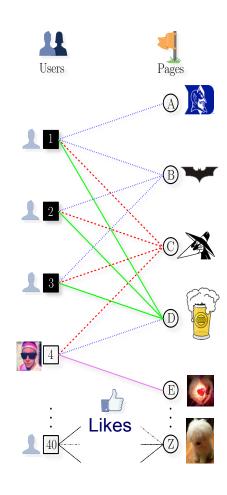


CopyCatch: Stopping Group Attacks by Spotting Lockstep Behavior in Social Networks, Alex Beutel, Wanhong Xu, Venkatesan Guruswami, Christopher Palow, Christos Faloutsos *WWW*, 2013.



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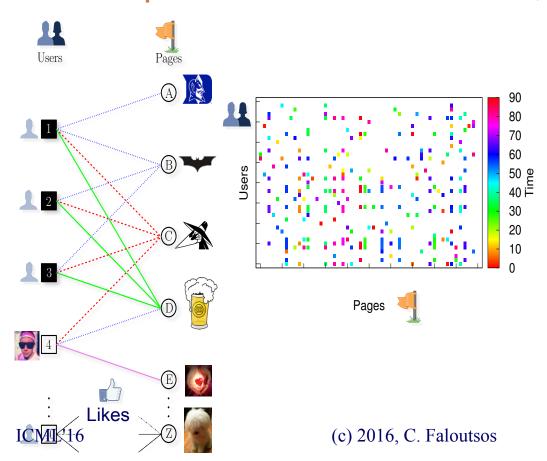


CopyCatch: Stopping Group Attacks by Spotting Lockstep Behavior in Social Networks, Alex Beutel, Wanhong Xu, Venkatesan Guruswami, Christopher Palow, Christos Faloutsos *WWW*, 2013.



Graph Patterns and Lockstep Our intuition Behavior

Lockstep behavior: Same Likes, same time

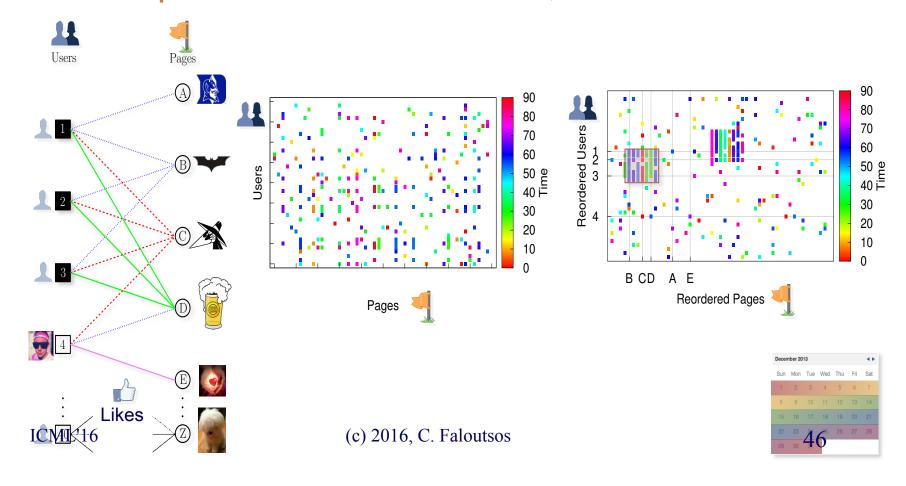






Graph Patterns and Lockstep Our intuition Behavior

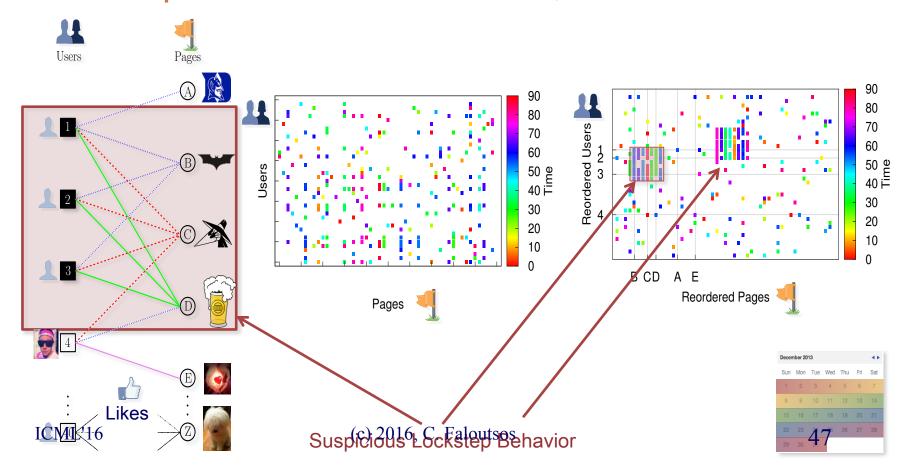
Lockstep behavior: Same Likes, same time





Graph Patterns and Lockstep Our intuition Behavior

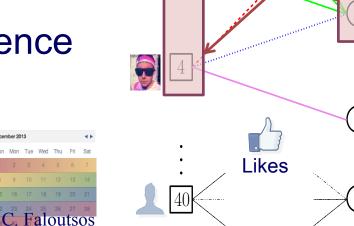
Lockstep behavior: Same Likes, same time





MapReduce Overview

- Use Hadoop to search for many clusters in parallel:
 - Start with randomly seed
 - 2. Update set of Pages and center Like times for each cluster
 - 3. Repeat until convergence





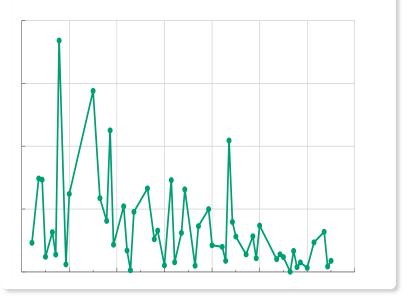


Deployment at Facebook

 CopyCatch runs regularly (along with many other security mechanisms, and a large Site Integrity team)

3 months of CopyCatch @ Facebook

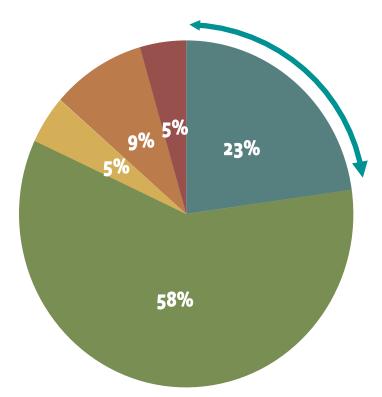
#users caught



time



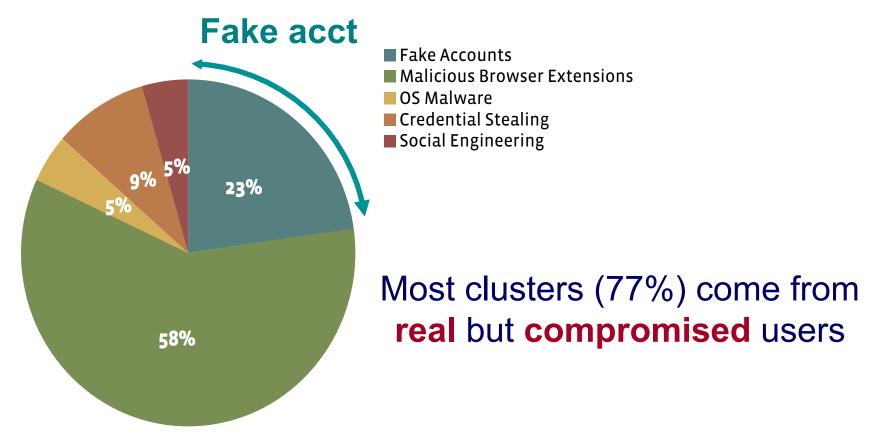
Deployment at Facebook



Manually labeled 22 randomly selected clusters from February 2013



Deployment at Facebook



Manually labeled 22 randomly selected clusters from February 2013



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 - CopyCatch
 - Spectral methods ('fBox')
 - Belief Propagation
- Part#2: time-evolving graphs; tensors
- Conclusions







Problem: Social Network Link Fraud

Target: find "stealthy" attackers missed by other algorithms

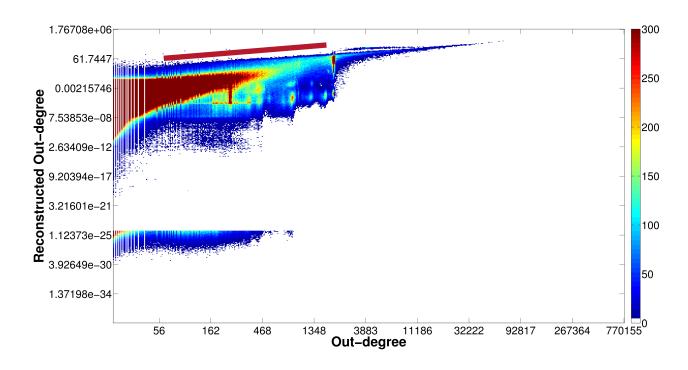


Clique

41.7M nodes 1.5B edges



Bipartite core



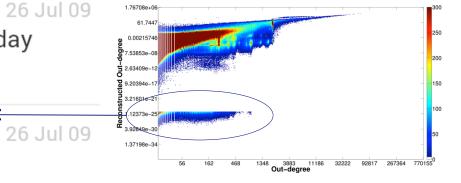


Problem: Social Network Link Fraud

Target: find "stealthy" attackers missed by other algorithms



Lekan Olawole Lowe @loweinc 26
Sign up free and Get 400 followers a day using http://tweeteradder.com





Lekan Olawole Lowe @loweinc Get 400 followers a day using http://www.tweeterfollow.com







Neil Shah, Alex Beutel, Brian Gallagher and Christos Faloutsos. Spotting Suspicious Link Behavior with fBox: An Adversarial Perspective. ICDM 2014, Shenzhen, China.



Roadmap

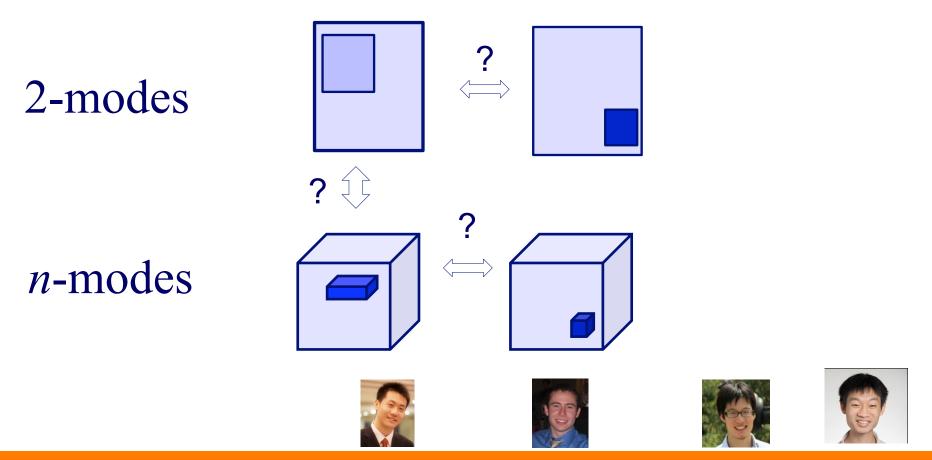
- Introduction Motivation
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 - Spectral methods ('fBox', suspiciousness)
 - Belief Propagation
- Part#2: time-evolving graphs; tensors
- Conclusions







Suspicious Patterns in Event Data



A General Suspiciousness Metric for Dense Blocks in Multimodal Data, Meng Jiang, Alex Beutel, Peng Cui, Bryan Hooi, Shiqiang Yang, and Christos Faloutsos, *ICDM*, 2015.



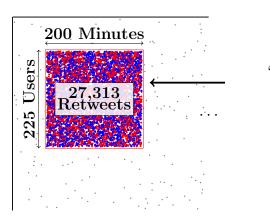
Suspicious Patterns in Event Data

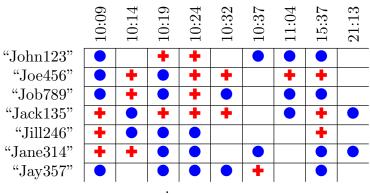
Which is more suspicious?

225 Users 20,000 Users Retweeting same 20 tweets Retweeting same 1 tweet 15 times each 6 times each VS. All in 3 hours All in 10 hours All from 2 IP addresses Answer: volume * D_{KL}(p|| p_{background}) ICML'1



Suspicious Patterns in Event Data







Retweeting: "Galaxy Note Dream Project: Happy Happy Life Traveling the World"

| | # | User × tweet × IP × minute | Mass c | Suspiciousness |
|------------------|---|--|--------|----------------|
| | 1 | $14 \times 1 \times 2 \times 1,114$ | 41,396 | 1,239,865 |
| CROSSSPOT | 2 | $225 \times 1 \times 2 \times 200$ | 27,313 | 777,781 |
| | 3 | $8\times2\times4\times1,872$ | 17,701 | 491,323 |
| | 1 | $24\times6\times11\times439$ | 3,582 | 131,113 |
| HOSVD | 2 | $18\times4\times5\times223$ | 1,942 | 74,087 |
| | 3 | $14 \times 2 \times 1 \times 265$ | 9,061 | 381,211 |

Carnegie Mellon

Roadmap

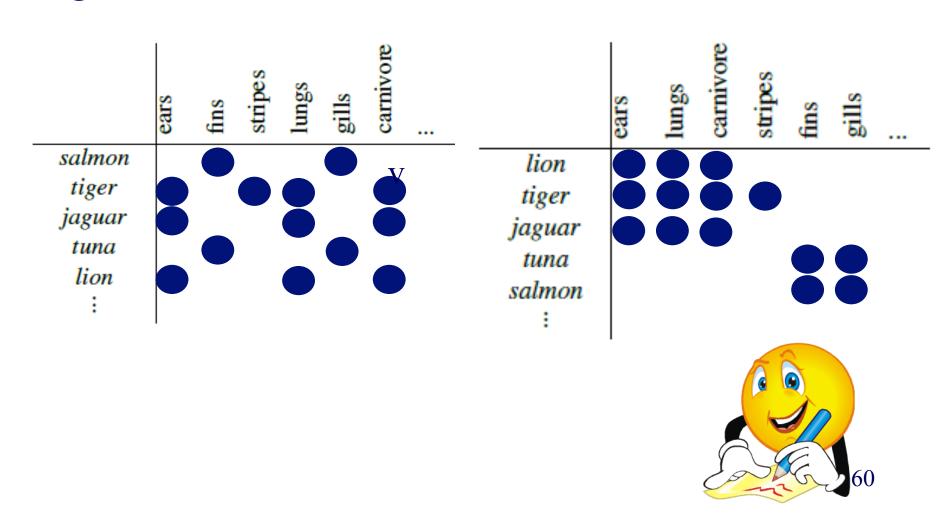
- Introduction Motivation
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 - Spectral methods ('fBox')
 - (Matrix re-ordering + education -> 'groupNteach')
 - Belief Propagation
- Part#2: time-evolving graphs; tensors
- Conclusions





Problem dfn:

e.g.





Problem definition

- **Given** a large binary matrix of facts of *(object, property)* pairs
- **Find** *groupings* of the facts and the *order* of transmission
- To **optimize** 'student effort' (-> incremental learning curve, 'ALOC')









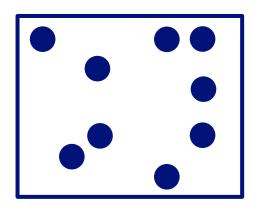
Bryan Hooi, Hyun Ah Song, et al, "Matrices, Compression, Learning Curves: Formulation, and the GroupNTeach Algorithms", PAKDD 2016



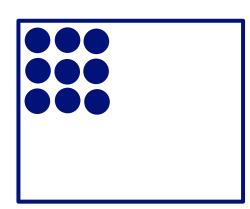
Details:

Given a large binary matrix of objects and properties, re-order rows and columns,

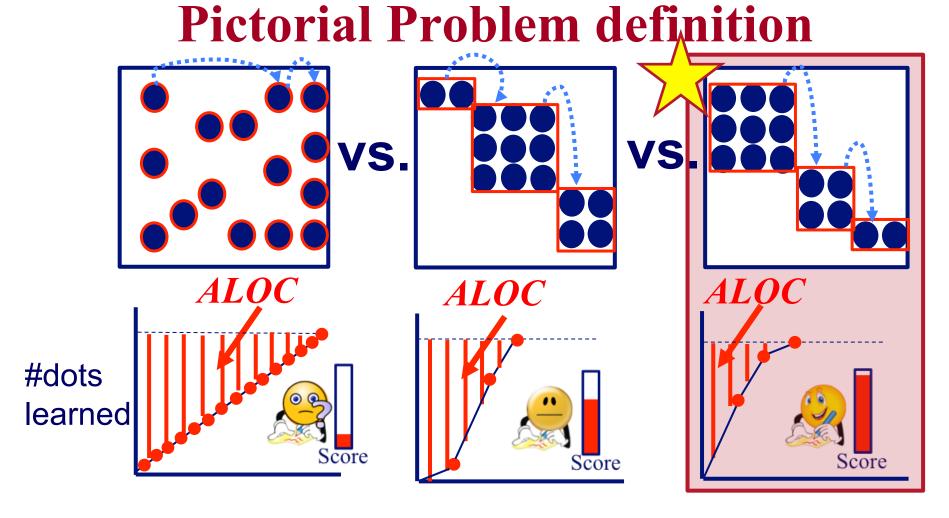
- **G1. Metric** for better encoding of matrix for student learning?
- G2. How do we construct language to describe it?
- G3. How do we optimize this metric?



VS.



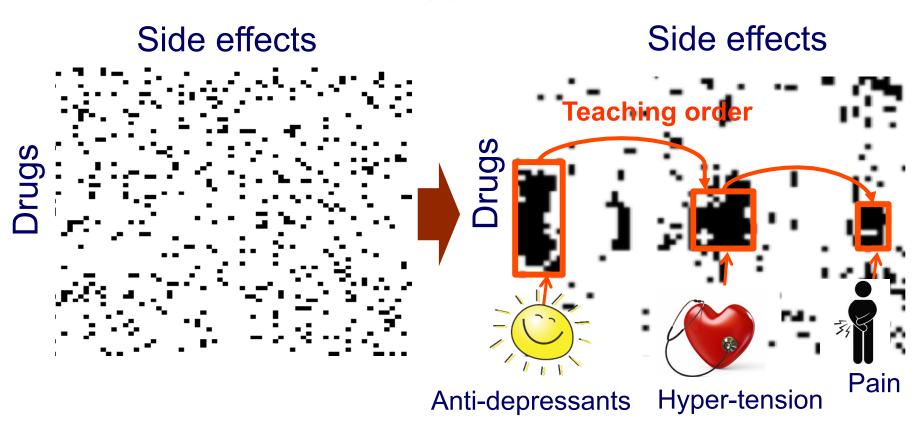




#bits transmitted



Results





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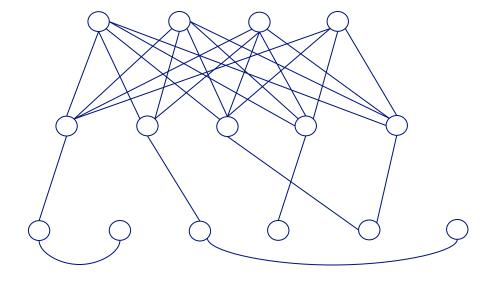


E-bay Fraud detection



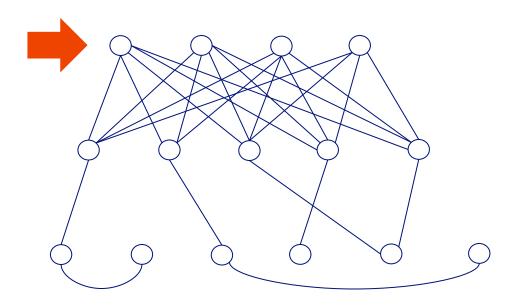


w/ Polo Chau & Shashank Pandit, CMU [www'07]



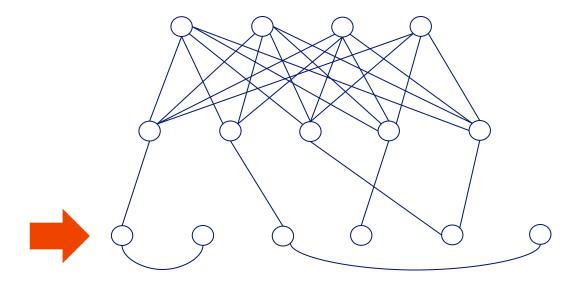


E-bay Fraud detection



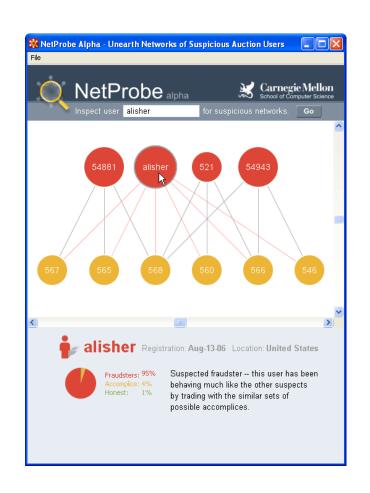


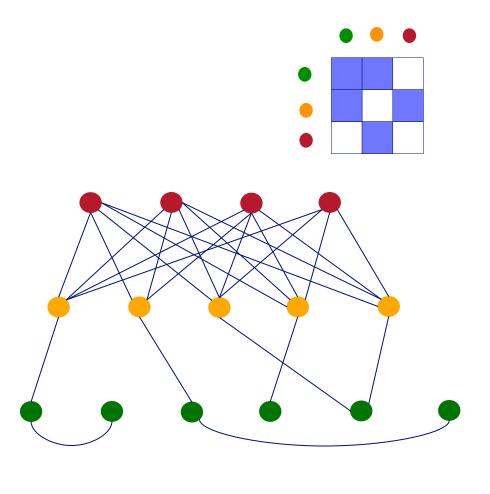
E-bay Fraud detection





E-bay Fraud detection - NetProbe







Popular press



The Washington Post

Ios Angeles Times

And less desirable attention:

• E-mail from 'Belgium police' ('copy of your code?')



Roadmap

- Introduction Motivation
- Part#1: Patterns in graphs
 - Patterns
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 - Spectral methods ('fBox')
 - Belief Propagation; fast computation & unification
- Part#2: time-evolving graphs; tensors
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Unifying Guilt-by-Association Approaches: Theorems and Fast Algorithms



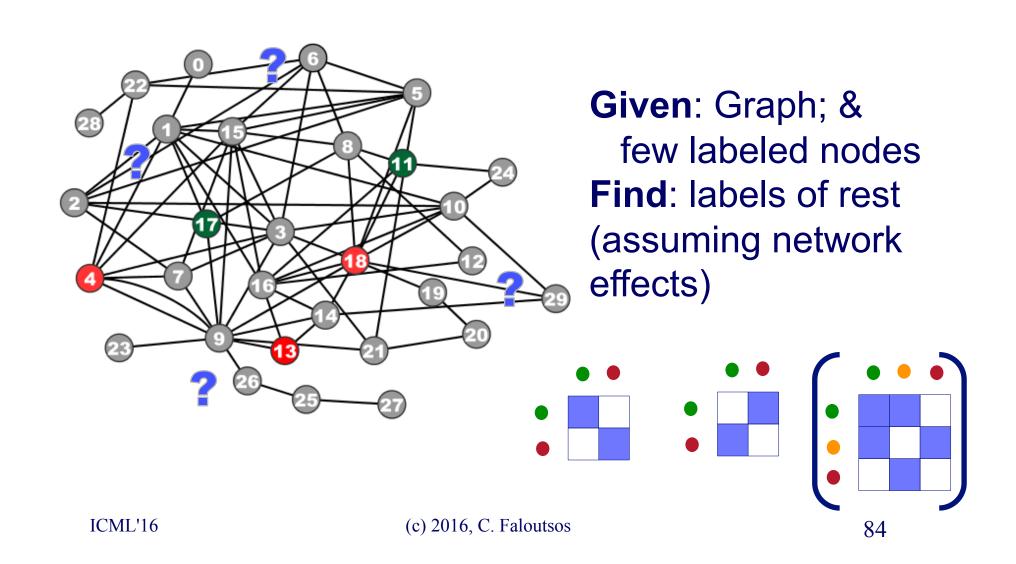
Danai Koutra
U Kang
Hsing-Kuo Kenneth Pao

Tai-You Ke Duen Horng (Polo) Chau Christos Faloutsos

ECML PKDD, 5-9 September 2011, Athens, Greece



Problem Definition: GBA techniques





Are they related?

- RWR (Random Walk with Restarts)
 - google's pageRank ('if my friends are important, I'm important, too')
- SSL (Semi-supervised learning)
 - minimize the differences among neighbors
- BP (Belief propagation)
 - send messages to neighbors, on what you believe about them

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Are they related? YES!

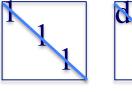
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 - minimize the differences among neighbors
- BP (Belief propagation)
 - send messages to neighbors, on what you believe about them

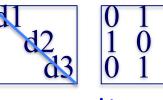
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Correspondence of Methods

| Method | Matrix | Unknown | | known |
|--------|---|--------------------------------|---|---------------------|
| RWR | $[\mathbf{I} - \mathbf{c} \ \underline{\mathbf{A}}\mathbf{D}^{-1}]$ | × x | = | $(1-c)\mathbf{y}$ |
| SSL | $[\mathbf{I} + \mathbf{a}(\mathbf{D} - \underline{\mathbf{A}})]$ | × x | = | \mathbf{y} |
| FABP | $[\mathbf{I} + a \mathbf{D} - c' \underline{\mathbf{A}}]$ | \times b _h | = | $\Phi_{\mathbf{h}}$ |



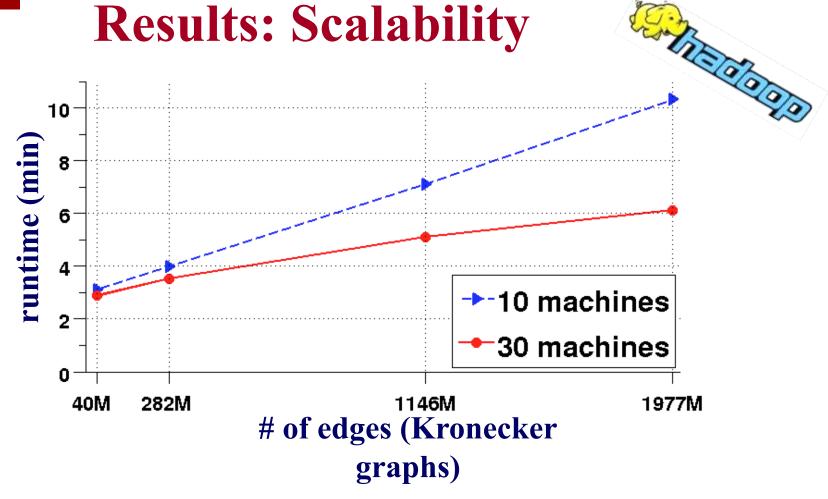


adjacency matrix









FABP is linear on the number of edges.

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Summary of Part#1

- *many* patterns in real graphs
 - Power-laws everywhere
 - Gaussian trap
 - Avg << Max



 Long (and growing) list of tools for anomaly/ fraud detection





Roadmap

- Introduction Motivation
- Part#1: Patterns in graphs



• Part#2: time-evolving graphs; tensors

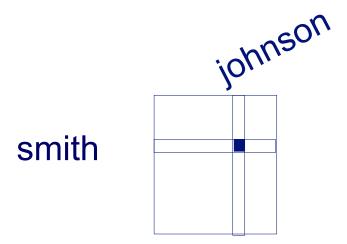


- P2.1: time-evolving graphs
- [P2.2: with side information ('coupled' M.T.F.)
- Speed]
- Conclusions

Part 2: Time evolving graphs; tensors



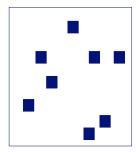
- Problem #2.1:
 - Given who calls whom, and when
 - Find patterns / anomalies



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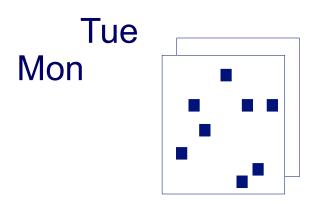
- Problem #2.1:
 - Given who calls whom, and when
 - Find patterns / anomalies



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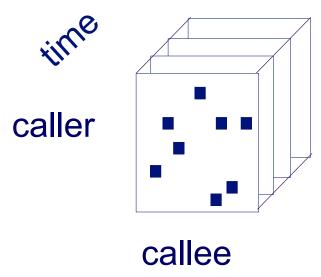
- Problem #2.1:
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- Problem #2.1:
 - Given who calls whom, and when
 - Find patterns / anomalies

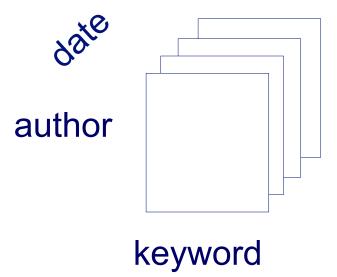


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- Problem #2.1':
 - Given author-keyword-date
 - Find patterns / anomalies



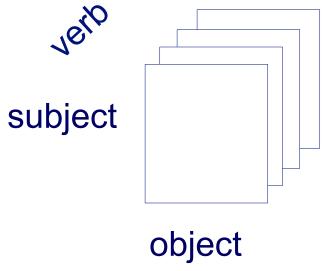
MANY more settings, with >2 'modes'

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- Problem #2.1'':
 - Given subject verb object facts
 - Find patterns / anomalies

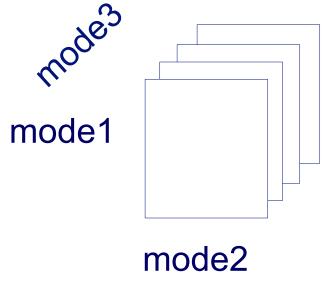


MANY more settings, with >2 'modes'

ICML'16



- Problem #2.1'':
 - Given <triplets>
 - Find patterns / anomalies



MANY more settings, with >2 'modes' (and 4, 5, etc modes)

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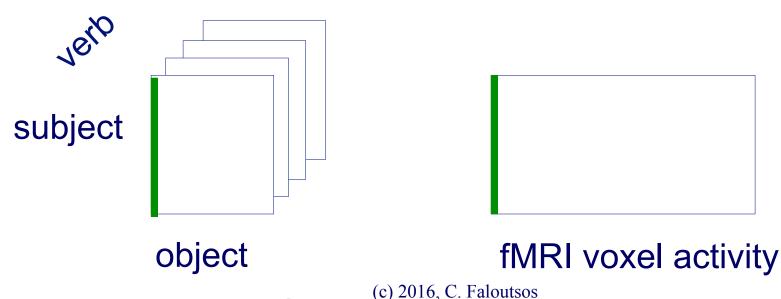
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Graphs & side info

- Problem #2.2: coupled (eg., side info)
 - Given subject verb object facts
 - And voxel-activity for each subject-word
 - Find patterns / anomalies



`apple tastes sweet'

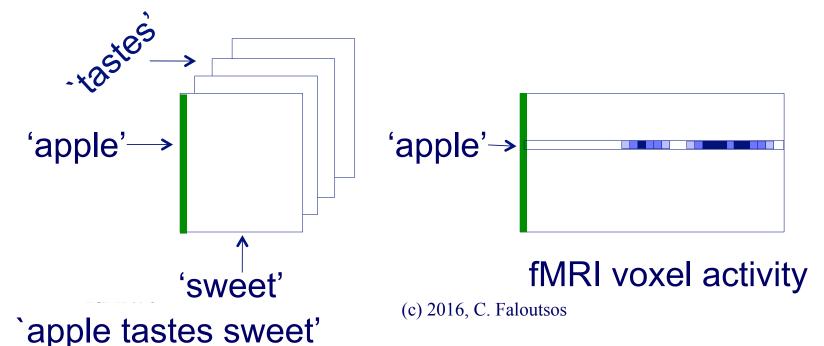
100





Graphs & side info

- Problem #2.2: coupled (eg., side info)
 - Given subject verb object facts
 - And voxel-activity for each subject-word
 - Find patterns / anomalies



101



Roadmap

- Introduction Motivation
- Part#1: Patterns in graphs



• Part#2: time-evolving graphs; tensors

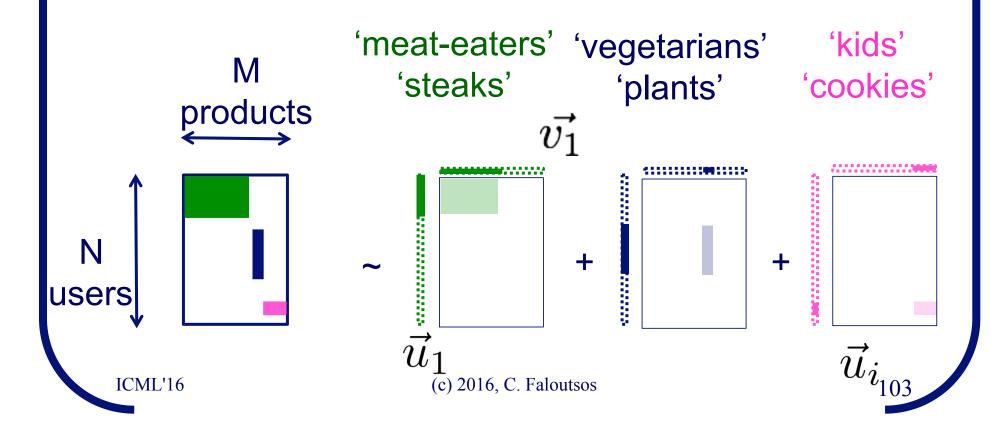


- P2.1: time-evolving graphs
- [P2.2: with side information ('coupled' M.T.F.)
- Speed]
- Conclusions



Answer to both: tensor factorization

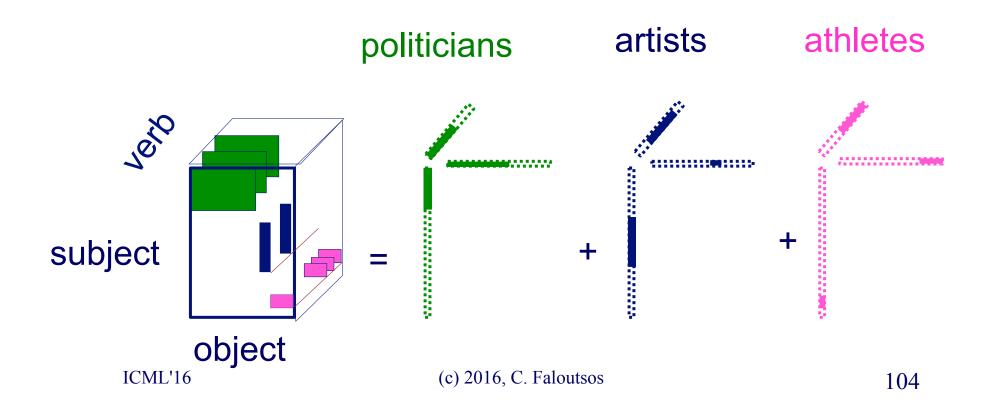
 Recall: (SVD) matrix factorization: finds blocks





Answer to both: tensor factorization

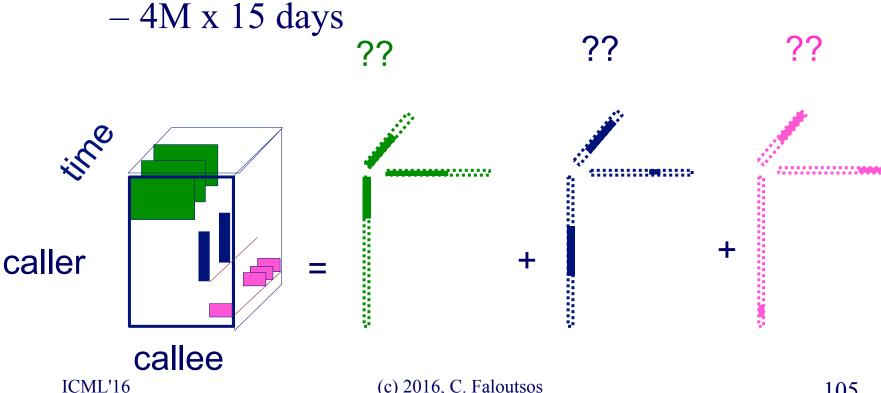
• PARAFAC decomposition





Answer: tensor factorization

- PARAFAC decomposition
- Results for who-calls-whom-when

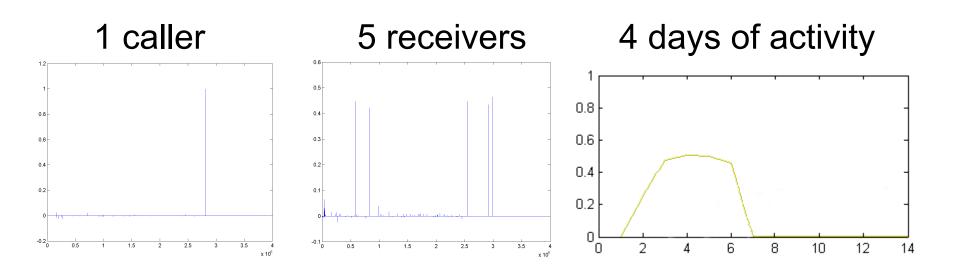


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Anomaly detection in timeevolving graphs =

- Anomalous communities in phone call data:
 - European country, 4M clients, data over 2 weeks



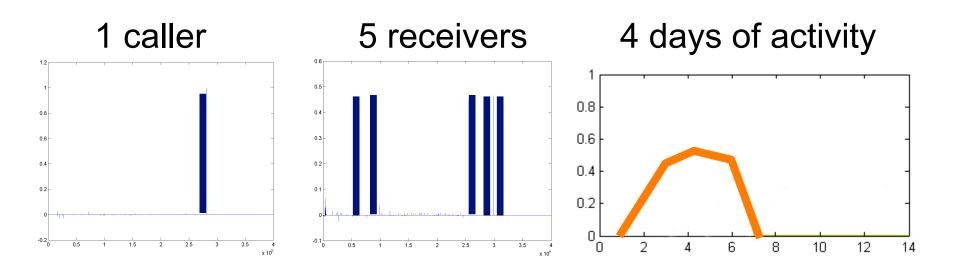
~200 calls to EACH receiver on EACH day!

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Anomaly detection in timeevolving graphs =

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~200 calls to EACH receiver on EACH day!

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Anomaly detection in timeevolving graphs =

- Anomalous communities in phone call data:
 - European country, 4M clients, data over 2 weeks







Miguel Araujo, Spiros Papadimitriou, Stephan Günnemann, Christos Faloutsos, Prithwish Basu, Ananthram Swami, Evangelos Papalexakis, Danai Koutra. *Com2: Fast Automatic Discovery of Temporal (Comet) Communities*. PAKDD 2014, Tainan, Taiwan.





Roadmap

- Introduction Motivation
- Part#1: Patterns in graphs



- Part#2: time-evolving graphs; tensors
 - P2.1: Discoveries @ phonecall network

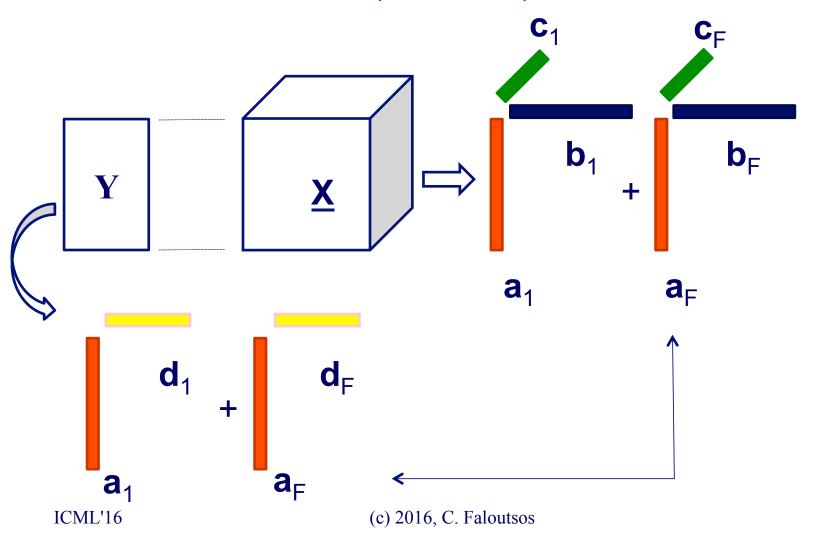


- [P2.2: Discoveries in neuro-semantics
- Speed]
- Conclusions

SKIP

Coupled Matrix-Tensor Factoriza

(CMTF)

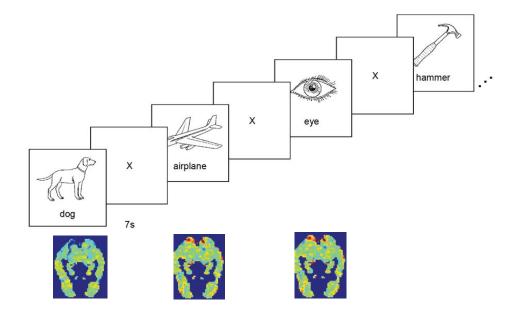








- Brain Scan Data*
 - 9 persons
 - 60 nouns
- Questions
 - 218 questions
 - 'is it alive?', 'can you eat it?'





*Mitchell et al. *Predicting human brain activity associated with the meanings of nouns*. Science,2008. Data@

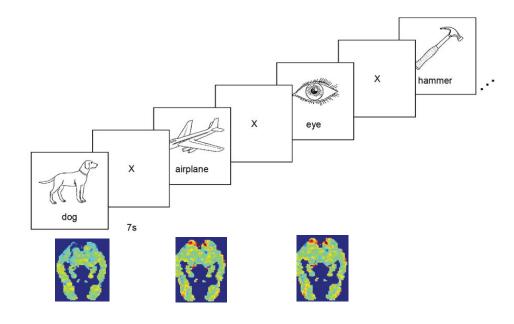
<u>www.cs.cmu.edu/afs/cs/project/theo-73/www/science2008/data.html</u>







- Brain Scan Data*
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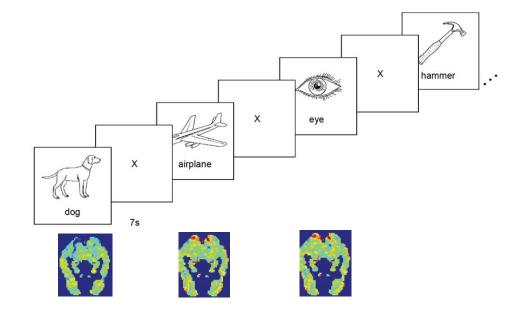
Patterns?





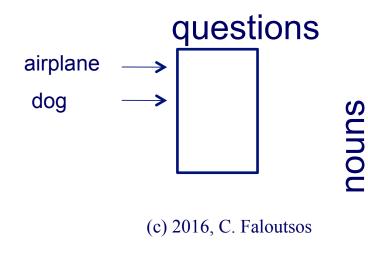


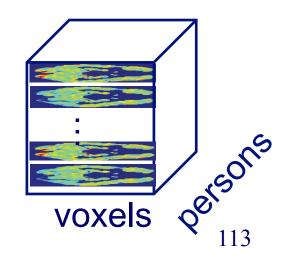
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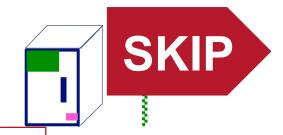
Patterns?

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Neuro-semantics

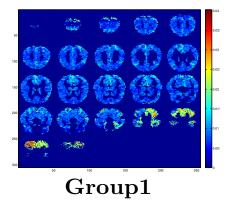


Nouns

beetle pants bee

Questions

can it cause you pain? do you see it daily? is it conscious?

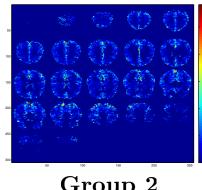


Nouns

bear cow coat

Questions

does it grow? is it alive? was it ever alive?



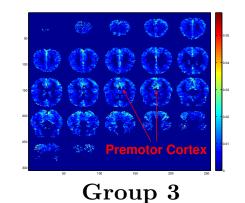
Group 2

Nouns

glass tomato bell

Questions

can you pick it up? can you hold it in one hand? is it smaller than a golfball?'

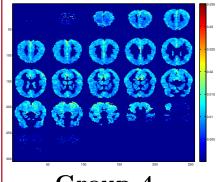


Nouns

bed house car

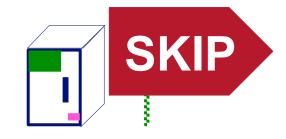
Questions

does it use electricity? can you sit on it? does it cast a shadow?



Group 4

Neuro-semantics



Small items -> Premotor cortex

Nouns

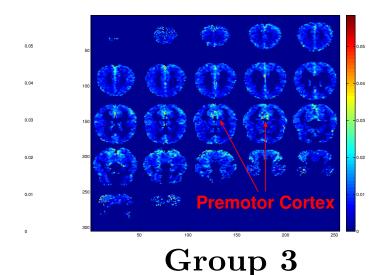
glass

tomato

bell

Questions

can you pick it up? can you hold it in one hand? is it smaller than a golfball?'





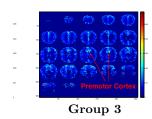
Neuro-semantics



Small items -> Premotor cortex

Nouns glass tomato bell Questions

can you pick it up? can you hold it in one hand? is it smaller than a golfball?'







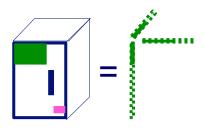


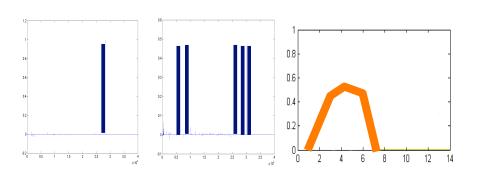
Evangelos Papalexakis, Tom Mitchell, Nicholas Sidiropoulos, Christos Faloutsos, Partha Pratim Talukdar, Brian Murphy, *Turbo-SMT: Accelerating Coupled Sparse Matrix-Tensor Factorizations by 200x*, SDM 2014



Part 2: Conclusions

- Time-evolving / heterogeneous graphs -> tensors
- PARAFAC finds patterns
- (GigaTensor/HaTen2 -> fast & scalable)





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Roadmap

- Introduction Motivation
 - Why study (big) graphs?
- Part#1: Patterns in graphs
- Part#2: time-evolving graphs; tensors







Thanks

















Disclaimer: All opinions are mine; not necessarily reflecting the opinions of the funding agencies

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Akoglu, Leman





Kang, U



Araujo, Miguel



Koutra, Danai





Beutel, Alex

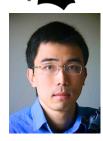




Papalexakis, Vagelis

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Chau, Polo



Shah, Neil



Hooi, Bryan



Song, Hyun Ah 120

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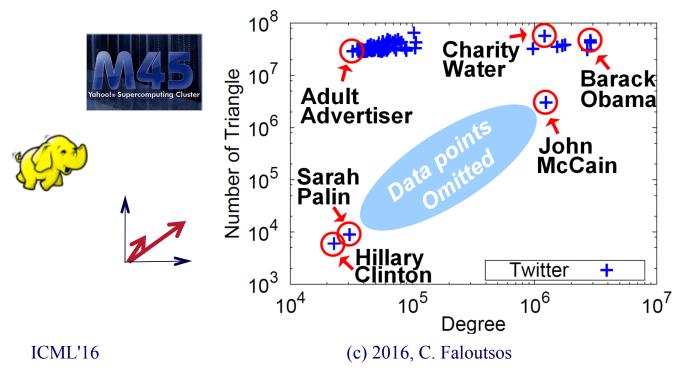
CONCLUSION#1 – Big data

Patterns Anomalies



• Large datasets reveal patterns/outliers that are invisible otherwise

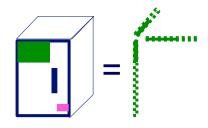
121

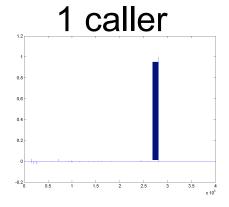


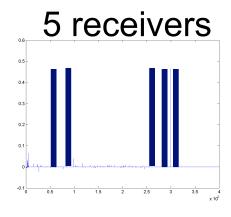


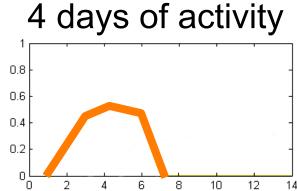
CONCLUSION#2 – tensors

powerful tool







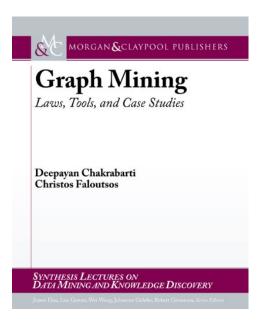


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References

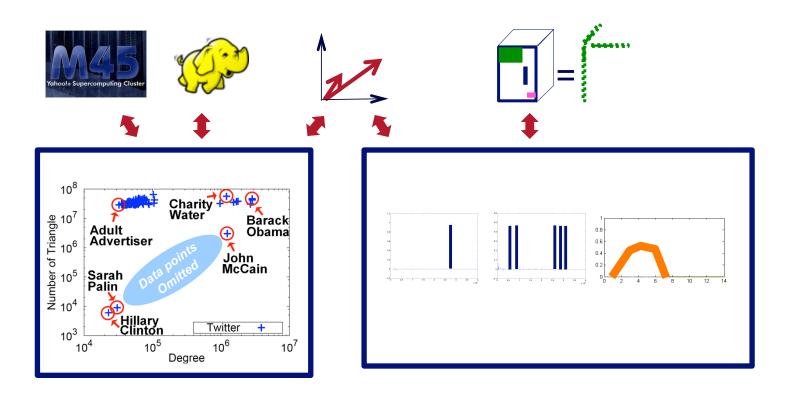
- D. Chakrabarti, C. Faloutsos: *Graph Mining Laws, Tools and Case Studies*, Morgan Claypool 2012
- http://www.morganclaypool.com/doi/abs/10.2200/ S00449ED1V01Y201209DMK006





TAKE HOME MESSAGE:

Cross-disciplinarity

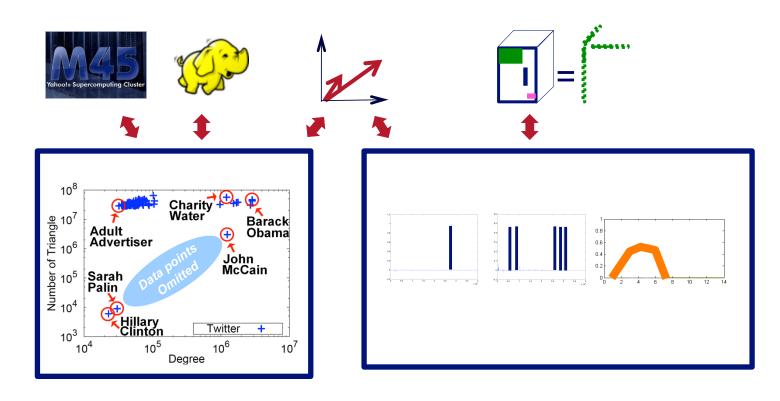


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Thank you!

Cross-disciplinarity



http://www.cs.cmu.edu/~christos/TALKS/16-06-19-ICML/